Stardust-NExT, Deep Impact, and the accelerating spin of 9P/Tempel 1.

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ABSTRACT

The evolution of the spin rate of comet 9P/Tempel 1 through two perihelion passages (CYs 2000 and 2005) is determined from 1922 Earth-based observations taken over a period of 13y as part of a World-Wide observing campaign and 2888 observations taken over a period of 50d from the Deep *Impact* spacecraft. We determine the following sidereal spin rates (periods): 209.023 ± 0.025 °/day (41.335 ± 0.005 h) prior to the 2000 perihelion passage, 210.448±0.016 °/day (41.055 ± 0.003 h) for the interval between the 2000 and 2005 perihelion passages, 211.856± 0.030 °/day (40.783± 0.006 h) from Deep *Impact* photometry just prior to the 2005 perihelion passage, and 211.625± 0.012 °/day (40.827± 0.002 h) in the interval 2006-2010 following the 2005 perihelion passage. The period decreased by 16.8 ± 0.3 min during the 2000 passage and by 13.7 ± 0.2 min during the 2005 passage suggesting a secular decrease in the net torque. The change in spin rate is asymmetric with respect to perihelion with the maximum net torque being applied on approach to perihelion. The Deep *Impact* data alone show that the spin rate was increasing at a rate of 0.024±0.003 °/d/d at JD2453530.60510 (i.e., 25.134 d before impact) and provides independent confirmation of the change seen in the Earth-based observations.

The rotational phase of the nucleus at times before and after each perihelion and at the *Deep Impact* encounter is estimated based on the Thomas *et al.* pole and longitude system (2007, Icarus 187, 4-15). The possibility of a 180° error in the rotational phase is assessed and found to be significant.

Analytical and physical modeling of the behavior of the spin rate through of each perihelion is presented and used as a basis to predict the rotational state of the nucleus at the time of the nominal (*i.e.*, prior to February 2010) *Stardust-NExT* encounter on 2011 February 14 20:42.

We find that a net torque in the range of $0.3-2.5 \times 10^7 \text{ kg.m}^2.\text{s}^{-2}$ acts on the nucleus during perihelion passage. The spin rate initially slows down on approach to perihelion and then passes through a minimum. It then accelerates rapidly as it passes through perihelion eventually reaching a maximum post-perihelion. It then decreases to a stable value as the nucleus moves away from the sun. We find that the pole direction is unlikely to precess by more than $\sim 1^{\circ}/\text{perihelion}$ passage. The trend of the period with time and the fact that the modeled peak torque that occurs before perihelion is in agreement with published accounts of trends in water production rate and suggests that widespread H_2O out-gassing from the surface is largely responsible for the observed spin-up.

1. Introduction.

In their assessment of the spin state of 9P/Tempel 1 following the *Deep Impact* encounter A'Hearn et al. (2005) found a sidereal period of 1.701 ± 0.014 d (211.6 ±1.7°/d). Thomas et al., (2007) determined the sense of spin to be direct and the preliminary pole position was RA = 5°, Dec = +78° (± 10° on the sky) roughly 11° from one of the two, photometrically degenerate, directions (46°, +73°) found earlier by Belton et al. (2005) using ground-based photometry. A'Hearn et al. also noted that the pre-impact rotation period of 1.744 \pm 0.006 days determined by Belton et al. (2005) differed significantly from the spacecraft value and suggested that the difference might be explained by an inadvertent shift in the analysis of earth-based data by a half or whole cycle between observing runs. Later, Belton et al. (2006) improved the Deep Impact sidereal period estimate to 1.6976 ± $0.0096 \text{ d} (212.06 \pm 1.2 ^{\circ}\text{/d})$ and Thomas et al (2007) revised the pole position (J2000) to RA = 294°, Dec = 73° (± 5° on the sky). Thomas *et al.* also set the prime meridian as $W(t) = 252.63^{\circ} + 212.064^{\circ} t$, where t is the number of days since the standard epoch (JD 2451545.0). W(t) is the angle between the chosen prime meridian and the intersection of the body equator and the standard Earth equator and defines the rotational phase of the nucleus at time t. This latter formula assumes a constant rotation period of 1.6976 d between the time of impact (JD 2453555.73928) and the standard epoch.

The small difference between the pre-impact rotation rate and the spacecraft value would have been of little concern had it not been for the recognition by J. Veverka and his colleagues that the *Stardust* spacecraft, which

had recently encountered comet 81P/Wild 2 (Brownlee *et al.*, 2004), was hibernating in deep space, could be revived, and had enough propulsion capability to reach 9P/Tempel 1 for an encounter on 2011 February 14. This mission, now called *Stardust-NExT*, was selected as a *Discovery* mission of opportunity by NASA (www.astro.cornell.edu/next/Science.htm). A Level 1 science requirement of this mission is to "Image 25% of the surface previously observed in the *Deep Impact* mission at better than 80 m/pixel" in order to look for changes in the condition of the surface that might have occurred during the previous perihelion passage (2011 January 12.2). A secondary science goal is to image the, as yet unseen, artificial crater formed during the *Deep Impact* mission that is located at 350.4W, -29.1 (Thomas, 2010, private communication). To ensure that these objectives can be met, a high-precision rotational ephemeris and an assessment of its stability is required and it is for this reason that the present study was initiated.

In subsequent preparations for the *Stardust-NExT* mission it was noted that the *Deep Impact* rotation rate calculated by Belton *et al.* (2006) did not correctly phase the light curves obtained some 14 months earlier from the *Hubble* and *Spitzer* Space telescopes (Lamy *et al.*, 2007; Lisse *et al.*, 2005). This was the first quantitative indication that comet 9P's rotation might be changing as it approached perihelion.

The theoretical basis for short timescale changes in cometary spin has been emphasized by Jewitt (1997; also summarized in Jewitt, 2004; see also Samarasinha *et al.* 2004) and exploratory calculations of excitation timescales

have been carried out by Gutiérrez *et al.* (2002), Jorda and Gutiérrez (2002), and Gutiérrez and Davidsson (2007). For a small (effective radius = 3.0 ± 0.1 km; Thomas *et al.*,2007), underdense (bulk density ~ 400 kg.m⁻³; Richardson *et al.* 2007) nucleus with a water production rate of 6 x 10^{27} molecules/s (Schleicher *et al.*, 2006) the timescale for substantial changes in the spin state is ~ 90 y based on Jewitt's formulation of spin-up time and his conjecture that the typical dimensionless moment arm for torques is ~0.05. Thus, from a theoretical point of view it should not be surprising if 9P/Tempel 1 was changing its current period by ~ 1% (0.4 h) in a single perihelion pass or if the direction of the rotation pole drifted by a degree or two.

There is also a growing observational base to support the measurable presence of this effect in comets. Drahus and Waniak (2006) have shown through the introduction of a novel photometric time-series analysis technique that the rotation rate of the distant comet C/2001 K5 (LINEAR) was perceptibly spinning-down as it receded from perihelion passage. In addition, earlier studies have found evidence of possible changes in spin rate in comets 10P/Tempel 2 and 6P/d'Arrest (Mueller and Ferrin, 1996; Gutiérrez et al., 2003). Other evidence of the action of rotational torques includes the cases of comets 1P/Halley, 2P/Encke and 29P/Schwassmann-Wachmann 1 each of which have been found to be in rotationally excited states (Belton et al., 1991; Samarasinha and A'Hearn, 1991; Meech et al., 1993; Belton et al., 2005).

Deep Impact photometry and imaging data from the ongoing Worldwide

Earth-based campaign on 9P/Tempel 1 (Meech et al, 2005, 2011) plus an early

Hubble Space Telescope study by Lamy et al. (2001) provide an unprecedented set of data with which to investigate the stability of the spin state of 9P/Tempel 1. The data that we use from ground-based and HST sources are described in Section 2 where we separate them into three groups: Region A (1997-1999), Region B (2001-2004) and Region C (2006 – 2010). This allows us to document the changes that occurred during the 2000 and 2005 perihelion passages. In Section 3 we present the *Deep Impact* approach photometry that we use to obtain direct evidence for an acceleration of the spin rate. In Section 4 we provide the theoretical basis and assumptions used in the analysis of the data. In section 5 we outline the rotational analysis and present the basic results on the spin rate of the nucleus and its rotational phase. In section 6 we discuss the dynamical evolution of the comet's spin state and construct analytical models for its changes through perihelion passage. In Section 7, we provide a general discussion of the relationship of our results with previously published studies of the comet's H₂O production rate. We also use our results to predict the rotation state we expect will be experienced by the Stardust-NExT mission at its encounter with 9P/Tempel 1 on 14 Feb, 2011. Section 8 contains a summary of our primary conclusions.

2. Earth-based observations and two independent methods of analysis.

In an accompanying paper, Meech et al. (2011) provide a detailed description of the Deep Impact World-Wide campaign, its goals, participant contributions, observations and results. In Fig.1 we show $R(1,1,\alpha)$ magnitudes for the entire data set after reduction to unit heliocentric and geocentric distance and where a is the solar phase angle. The rise and fall of the coma brightness around perihelion dominates the figure and the substantial effect of diminishing solar phase angle at the oppositions of 2000, 2002, 2003, 2004, 2006, 2008 and 2010 is clear. A small sub-set of this data was obtained as V magnitudes and these have been converted to R magnitudes using (V-R) = 0.50 mag (Li et al., 2007). Embedded in this data set are the results of three studies done with the *Hubble* Space Telescope (HST). These were obtained in 1997 (Lamy et al., 2001), 2004 (Lamy et al., 2007) and 2009 (Meech et al., 2011). The latter two were done at the request of the *Deep Impact* team in order to obtain data of sufficient quality to distinguish between alias periodicities and to measure, with the highest possible accuracy, the rotational phase of the nucleus at each epoch. The $V(1,1,\alpha)$ magnitudes in Lamy et al. (2007) were converted to R(1,1, α) as noted above.

All of the above photometric reductions depend on orbital information obtained from the JPL Horizons site (http://ssd.jpl.nasa.gov/?horizons) using the default orbit solution (K054/15) for 9P/Tempel 1. The complete set of reduced ground-based data, relevant geometry, and the timing used in this paper is listed in a supplementary electronic data file appended to Meech *et al.* (2011). In our

analysis we divided the data into three intervals each of which was expected to yield significantly different values for the spin rate: Region A, before the year 2000 perihelion passage; Region B, between the 2000 and 2005 perihelion passages; and Region C, post the 2005 perihelion passage. A fourth region D was reserved to cover the time post the 2011 perihelion passage and through the *Stardust-NExT* encounter on 14 Feb, 2011.

Correction for solar phase angle brightness effects. Li et al. (2007) have determined the disk integrated phase function of 9P to be β = 0.046 ± 0.007 mag./deg for 4° < α < 117°. Earlier Belton et al. (2005), using data obtained between 1997 and 2002, found evidence for an increase in β inside of 4°. They represented the phase law as a polynomial (Δ R(1,1, α) = -0.0180955 - 0.250260 α + 0.0306201 α ² - 0021805 α ³ + 0.0000798 α ⁴ - 0.0000015 α ⁵ mag.) good for α < 15°. In Fig. 2 the data and these two phase laws are compared, but, as can be seen, a simple linear regression, R(1,1, α) = 14.905 + 0.0449 α mag, gives an excellent account of the current data for 1° < α < 14°. It is this latter relationship that we have used to correct the magnitude data to zero solar phase angle (Fig. 3).

In Figs. 3, 4 and 5 we show R(1,1,0) as a function of calendar year, time from perihelion passage, and heliocentric distance. In Fig. 3 we see how well the solar phase angle brightness effect has been removed. The scatter in magnitudes while the comet is near aphelion now primarily reflects the variation in brightness caused by the spin of 9P's irregularly shaped nucleus. In Fig. 4 we see how consistent the data are from one perihelion passage to the next. In Fig.

5 we see how the brightness of the coma is maintained at higher levels postperihelion relative to its behavior pre-perihelion, an effect seen in other comet light curves and that prevented our use of early post-perihelion observations in the determination of the rotational state.

Methods and preparation of the data for rotational analysis. Because of our intention to use the results of this study to adjust the arrival time of the Stardust-NExT spacecraft at the comet (and so meet Level 1 requirements specified by NASA) it was decided to perform two independent analyses for the predicted rotational state of the comet. While the details of each of these are reserved to a later section, we now give an overview of these independent techniques as an introduction.

The first was done at the Jet Propulsion Laboratory in Pasadena and was based on a least-squares fit of model light curves to each region of R(1,1,0). The model light curves were generated using a combination of the Thomas *et al.* (2007) shape model, a Hapke photometric function, SPICE orbital data (http://naif.jpl.nasa.gov/naif/data_comet.html), and an unexcited rotation model, *i.e.*, the spin axis was assumed fixed in space and coincident with the principal axis of maximum moment of inertia. Hapke parameters for 9P have been determined by Li *et al.* (2007), however, in certain applications that utilized intensive computations a Lommel-Seeliger (LS) function was substituted. The LS photometric function represents single (isotropic) scattering from a semi-infinite

medium and comparisons with Hapke calculations demonstrated that it was an excellent proxy for 9P which has a low surface albedo.

The second investigation, which was done in parallel with that at JPL, was done at Belton Space Exploration Initiatives, LLC, in Tucson. This study applied standard astronomical period finding techniques to R(1,1,0) after removing orbital synodic and solar phase angle timing (Harris et al., 1984) effects. The data set was transformed to one that would have been acquired by an inertial observer fixed relative to the comet. This analysis avoided the use of the shape model and the choice of a surface photometric function. Under normal circumstances cometary light curve data rarely extend over an interval longer than two or three months near a single opposition and such observations can be phased to determine an adequate approximation to the rotational period without first accounting for orbital synodic effects or worrying about a change in the timing of light curve maxima due to changing illumination geometry (Fig. 6). In fact, these corrections would be hard to make without prior knowledge of some of the physical properties of the nucleus. In the present case, such prior knowledge is available, i.e., the rotational period, the polar axis, the shape, and photometric behavior of the nucleus are all approximately known (Belton et al., 2005; Thomas et al., 2007; Li et al., 2007) and first order corrections can be made. Since the observations are, as shown in Fig. 7, spread over several oppositions that are widely separated around the orbit and involve a wide range of solar phase angles, accounting for these effects is essential to obtaining well-defined light curves and in achieving the highest accuracy in the sidereal spin rate.

Both of these investigations were subjected to periodic and independent peer reviews during the analysis. The internal peer review team included A. Harris, T. Duxbury and D. Scheeres.

3. Deep Impact approach photometry.

As noted in the introduction a number of estimates have been made of the rotational period of the nucleus based on the Deep Impact approach photometry. However, all of these where based on an early form of the photometry that was subsequently found to have short-comings that may have affected the results in the earliest parts of the approach sequence. These problems, which could possibly affect the accuracy of the estimated period, include estimation of the bias correction to the nearest DN (data number, a linear measure of the brightness), ignoring faint horizontal striping in the images, and ignoring small corrections to the photometry that are required when the comet happened to be placed on the two rows in the image surrounding the horizontal boundary between the upper and lower halves of the detector. These corrections have now been made (see appendix A for a more complete discussion) and a new, improved, version of the approach photometry made available for analysis. It consists of 595 points of "science" data covering 63.1d on approach and 2419 points of "navigation" data covering an interval of 49.8 d. The last datum in these sets was taken at 0.25 d before impact. All data considered here (2888 Science and Navigation observations taken from 50 to 0.25 d before impact) were taken with the Medium Resolution Instrument (MRI) through one or the other of two

CLEAR, effectively identical, filters with a central wavelength at 650 nm (Hampton *et al.*, 2005). The photometry, which refers to circular apertures 5, 7, 9, 15, 20, 25, and 30 pixels in diameter centered on the comet, can be found on the PDS Small bodies Node http://pdssbn.astro.umd.edu in the *Deep Impact* archives.

We assume that the light of nucleus, which was centered in the circular aperture, was completely contained within it. At 0.25 d before impact (the last datum) the mean diameter of the nucleus subtends 1.8 pixels; *i.e.,* the nucleus is always within our smallest aperture of 5 pixels. The DN at each time, t, consists of two parts: that contributed by the nucleus and that by the inner coma. We express the signal as:

DN (t) =
$$\beta$$
.C_n. f_n(α). F_n(t). r^{-2} .d⁻² + F_c(t, r, d, α)

Where β is a constant calibration factor, C_n is the mean brightness of the nucleus, f_n is the solar phase function (as determined in Section 2). $F_n(t)$ is the variation of the brightness of the nucleus as it rotates and r and d are the distances from the sun and the spacecraft in AU. F_c is the coma contribution to the signal and has a complex dependence on the parameters shown. With the exception of β , F_c and F_n all of the other quantities are specified. Our objective is to determine the product β . F_n and analyze its time dependency for the rotational period. To do this we must first separate β . F_n from F_c , which we assume to make a negligible *rotational* contribution to the signal. Unfortunately, this latter

assumption cannot be precisely true since the origin of coma material is tied to the surface of the nucleus and will initially share its motion. As the coma material flows out from the nucleus conservation of angular momentum will reduce its angular motion and periodicities may be introduced that are systematically different to that of the nucleus.

We have investigated the possible effect of this phenomenon by searching for coma variability in the difference signal between the 7 and 5 pixel apertures. This signal should arise entirely from the coma. For times close to impact, when the very inner coma is being sampled, we have detected variability at the nucleus period but with an amplitude that is ~0.1 that of the variability of the nucleus itself. At 10 days before impact, when a more distant and broader region of the coma is being sampled, coma variability is undetectable presumably being overwhelmed by noise. At 0.25 d before impact the coma signal in the 5 pixel aperture is only ~ 0.04 that of the nucleus (Fig. 8) and so the amplitude of the coma's observed variability contributes a negligible ~ 0.004 fraction of the total observed amplitude. At earlier times, well before impact and when the coma is the dominant component of the signal, the 5 pixel aperture integrates over a wide region of the coma presumably washing out any rotational variability from that source. In Fig. 8 we show the approximate contribution of the nucleus to the total signal in the 5 pixel diameter aperture. This first order separation of the nucleus from the coma was done by assuming that there is a linear relationship between the coma signal and aperture diameter in apertures 5 through 30. The signal extrapolated to D = 0 is a first order estimate of the contribution of the nucleus.

This simple coma model is based on a symmetric constant velocity outflow in the coma and a point nucleus and predicts the roughly linear dependence of the signal with aperture size that is seen in the data. The coma is seen to dominate until about 4 days before encounter and considerable care was taken to remove it before the rotational analysis.

The data consists of two groups: "Science" data and "Navigation" data whose time coverage, sampling, and mode of acquisition were quite distinct. While they are taken with the same instrument and filters they were taken in different camera modes as described in appendix A. Nevertheless, the two types of data were found to be photometrically consistent and we use them together as a "joint" data set. To illustrate the separation of coma from β.F_n and the "cleaned-up" data we plot, in Fig. 9, the normalized brightness, $r^2 d^2 DN/C_n f(\alpha)$, versus time from impact. C_n is taken as 100 units and r, d and α were obtained from the JPL Horizons system where the *Deep Impact* spacecraft is identified as "@ - 140". The coma and mean nucleus is represented as a 4th-order polynomial in each of the two cleaned-up data sets and then subtracted leaving the time variable component of the nucleus, β.F_n. In principle the mean level of this component should be constant and zero and this can be seen to be approximately the case in Fig. 9. The two data sets are then combined to form the joint version of $\beta.F_n$ shown in the lower panel of the figure.

4. Rotational equations of motion and assumptions

The action of forces generated by the momentum of gas and dust leaving the surface of an active comet nucleus can at any instant of time be decomposed into two parts: those which act at the center of mass of the body, F, and those which apply torques, T. Both forces are functions of time, t, and vary rapidly on a rotational time scale but are thought to vary relatively smoothly on an orbital time scale.

Occasionally major cometary events such as a splitting, or a major outburst, or the appearance or disappearance of a major active region, or a close encounter with a major solar system body may occur that lead to unpredictable changes in these forces. Such effects are not considered here and we assume that the rate of change of the average of T(t) over a rotational cycle, d < T(t) > /dt, changes smoothly over orbital timescales. It is not necessary that such orbital changes are the same from one orbit to another and we shall, in fact, find that they are not.

We assume that the nucleus rotates as a rigid body and the vector equation for the angular motion of such a body in a fixed frame, e.g., Rutherford, (1951), is:

$$dh/dt = T_{tidal}(t) + T(t)$$
 (1)

Where h is the angular momentum of the body and T_{tidal} are torques that come into play during near encounters with planets or the sun. In the present

application we shall assume that $T_{tidal} \equiv 0$. The net torque due to mass loss is therefore defined as:

$$T = \int (\rho \times q.V).dS$$
 (2)

where ρ is the position vector of an elemental area dS with respect to the center of mass of the nucleus, V(t) is the velocity of the outflow and q(t) is the net rate of mass loss from dS. The integration is over the entire surface and, although not specifically indicated in the notation, averaged over a rotational cycle. With ω as the angular velocity of the nucleus relative to fixed axes that momentarily coincide with the principle axes of inertia in the nucleus, Eq.1 yields Euler's equations of angular motion:

$$A^*d\omega_x/dt + (C^*-B^*).\omega_y\omega_z = [\int (\rho \times q.V).dS]_x$$

$$B^* d\omega_y / dt + (A^* - C^*) \cdot \omega_z \omega_x = [\int (\rho \times q.V) \cdot dS]_y$$
 (3)

$$C^*d\omega_z/dt + (B^*-A^*).\omega_x\omega_y = [\int (\rho \times q.V).dS]_z$$

Where A*, B*, and C* are the principal moments of inertia.

The assumption that a cometary nucleus rotates as a rigid body deserved some comment in light of the low cohesive strength found for cometary material in D/Shoemaker-Levy 9 (Asphaug and Benz, 1996) and 9P (Richardson *et al.*,

2007) and the proposition of Belton and Melosh (2009) that fluidized transport of substantial amounts of material may take place episodically in the interior ultimately leading to outbursts and surface flows. To justify our assumption it is sufficient to show that rotation is a minor source of stress and that the loss of material in a repetitive outburst has a minor effect on the moment of inertia. Near the ends of the long axis of 9P the gravity is ~0.027 cm/s² and the centripetal force is ~ -0.001cm/s² (Thomas, 2007; private communication) thus the rotational contribution is minor. We estimate the moment of inertia of the nucleus to lie between $0.8 - 4.6 \times 10^{19} \text{ kg.m}^2$ assuming a homogeneous mass distribution in the interior, a spherical approximation to the shape, and using the mass range determined by Richardson et al. (2007). A typical repetitive outburst releases about 10⁶ kg of material at the surface whose maximum contribution to the moment of inertia for a 3 km radius body is ~ 10¹³ kg.m². Since this is much less than the moment of inertia, the loss of material in a repetitive outburst, or similar events, will not have a noticeable effect on the rotational dynamics of the nucleus.

These equations provide a firm basis for detailed *ab initio* simulations of the evolution of the spin of the nucleus, if the inertias and mass loss are fully understood *e.g.,* Samarasinha and Belton (1995) or Gutiérrez and Davidsson (2007). The study of non-gravitational effects on 9P's orbit suggest that the direction of the spin axis is stable or, at most, slowly changing (Yeomans *et al.*, 2004b). In addition, the close similarity of the pole direction (RA, Dec = 294°, +73°; J2000) found by Thomas *et al.* (2007) from *Deep Impact* images of the

resolved nucleus with the pole direction (RA, Dec = 293°, =+73°) derived from the time dependence of coma features by Vincent et al. (2010) suggest that the direction of the polar axis is well determined. In addition the pole direction (RA, Dec = 46°, +73 revised to 317°, +81° in 2006) derived from light curves obtained over several years prior to the *Deep Impact* encounter (Belton et al., 2005) support the idea that any precessional drift in the pole direction is slow, i.e., not exceeding a few degrees on the sky per perihelion passage. Moreover, with the assumption of a homogeneous mass distribution in the nucleus, observations of the shape of the nucleus allow us to estimate the direction of the principal axis of maximum moment of inertia, which, within the errors of estimation, is found to be parallel and coincident with the estimated spin axis (Thomas et al. 2007). All of these observations support the idea that the spin of the comet is close to its fully relaxed state. Additional support comes from an analysis of periodicities in the Deep Impact light curve, which is found to yield only harmonics of a single period. While this does not ensure that the nucleus is in a fully relaxed state it is, nevertheless, a *necessary* condition. We conclude that the nucleus is apparently close to the state of simple rotation around its principal axis of maximum moment of inertia, which we take as C*. In this case the z-axis is coincident with the spin axis and we assume that $\omega_x = \omega_y = d\omega_x/dt = d\omega_y/dt = 0$. This assumption implies that, for over the period of the observations being considered, the direction of the rotation axis is considered fixed. We will revisit and provide a check on this assumption in Section 6.

After dropping the z subscript, Eqs. 3 reduce to:

$$d\omega(t)/dt = T(t) \tag{4}$$

where

$$T(t) = \int (\rho \times q.V).dS /C^*$$

averaged over a rotational cycle.

We define the *rotational phase*, W(t), of the nucleus at time, t, as the angular distance of the prime meridian, as defined by Thomas *et al.* (2007), to the meridian that contains the direction of the ascending node (RA, Dec = 23.80° , 0.0° ; J2000) as seen from the nucleus, *i.e.*,

$$dW(t)/dt = \omega(t) \tag{5}$$

Integrating from t₀ to t we get

$$W(t) = W_0 + \int_{t0.t} \omega(t).dt$$
 (6)

Since the sense of spin of 9P is observed to be *direct* (Thomas *et al.*, 2007), W(t) is the West longitude of the reference direction at time t. At the time of impact in the *Deep Impact* Mission (JD2453555.73928) Thomas *et al.* found that

$$W(t) = 252.63^{\circ} + 212.064^{*}(t - t_0)$$
 (7)

where the standard epoch is t_0 = JD2451545.0 and the assumed spin rate (212.064°/d) was constant between the standard epoch and the time of impact.

In the analysis that follows we make two further assumptions. First, we assume that for an extended period around aphelion (Regions A, B, C, D) do/dt =0, i.e., torques during that period are negligible. Secondly, we assume that the light curve of the nucleus, in the same extended period around perihelion, can be predicted from Thomas et al's. (2007) shape model. Referring to Eq. 6 and Fig. 3, the first of these assumptions implies that the following relationships exist:

$$W_i(t) = W_{0i} + S_i^*(t - t_0)$$
 j = Regions A, B, C, D (8)

and the rotational analysis in the next section is designed to discover W_{0j} and S_{j} for each of the regions.

The second of the above assumptions is more problematical because the 3-dimensional shape of 9P's nucleus is poorly defined over large areas of the nucleus. This is a direct result of the linear *Deep Impact* flyby geometry and the slow rotation of 9P. Tests of model predictions with *Deep Impact* approach photometry show that with either a Lommel-Seeliger or Hapke scattering function the Thomas shape model can give a good match to the observations. However, while the shape model gives good results for the light curve at most rotational phases, we find that there is a restricted range of rotational phase (see section 5 below) where the data and models are discordant.

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The validity of both of the above assumptions depends on the premise that there is an extended interval near aphelion when the effect of coma on the light curve and the dynamics of the nucleus is negligible. To assess the influence of the coma we first remove the mean brightness of the nucleus from the data shown in Fig. 3. The mean absolute R magnitude of the nucleus at zero solar phase angle is taken as 14.905 (see Section 2 for the origin of this value) and magnitudes are converted to relative brightness units with the mean brightness of the nucleus set at 100 units. In Fig. 10 the pre- and post-2005 perihelion coma brightness is compared to the mean brightness of the nucleus (shown as a dashed horizontal line). Pre-perihelion the signal is essentially coma free at distances beyond 3.2 AU where the RMS variability of ±15 units is mainly due to rotation. The error of an observation is typically ± 3.5 units. In the post-perihelion period only the data beyond 4.1 AU can be considered free of coma. The RMS spread at these distances is again ±15 units. The post-perihelion data between 3.6 and 3.9 AU is from the 2006 opposition and is ~ 42% due to coma. However, the RMS variation of ±17 units is roughly similar to the mean level found beyond 4.1 AU suggesting that the variability in 2006 remains dominated by rotation. A substantial observational effort was made during the September 2000 opposition to obtain rotational information when the comet was near 3 au post-perihelion. However, at that time the coma level was 2.7 times that of the nucleus and the RMS spread had increased to ± 55 units. Since the signature of nucleus rotation is expected to be at the ± 15 unit level, it is clearly overwhelmed by variability in

the coma. We have therefore omitted this part of the data from the rotational analysis.

5. Rotational analysis

We determine the values of W_{0j} and S_j (Eq. 8) for each region j using the two methods described earlier. They share identical data sets and the combined ground-based and HST data for each region are shown in Fig. 11. The *Deep Impact* data are already displayed in the bottom panel of Fig. 9. Descriptive information on the data is collected in Table1.

5.1 The JPL Method. This is simply a classical least squares fit of a rotation model to the measured photometry. For the more typical case of unaccelerated rotation, which is presumed between active periods, the model parameters are the rotation phase $W_{0j}=W_j(t_0)$ and rate $S_j=S_j(t_0)$ at some epoch t_0 . In this way the spin phase and rate were obtained from a simultaneous fit to the photometry, in contrast to the power spectrum analysis used in the Tucson method described below.

The least squares approach attempts to minimize the sum of squares of the photometric residuals, which are the differences between the observed and computed (O-C) magnitudes of the cometary nucleus at each measurement time. The observed photometry is reduced to R(1,1,0) values, while the computed magnitudes are obtained from a special-purpose synthetic light curve generation

tools ("runlcrv.cgi" and "runlcrv_hapke.cgi" provided by B. Carcich) that can be queried online.

The synthetic light curve tool takes as input the rotation history of the comet based on the assumed values of W_{0i} and S_i and returns the received flux at a list of requested observation times for a specified observing location. The position of the observer can be selected as the geocenter, *Deep Impact* spacecraft, Stardust-NExT spacecraft, Spitzer Space Telescope or Hubble Space Telescope. These tools use Lommel -Seeliger and Hapke scattering laws and the Thomas et al. (2007) shape model. They use a plate model for the comet shape to capture the illumination effects for the particular positions of the observer and the sun at the emit time, and the light time delay is fully incorporated in order to accurately represent the measured flux at the observation time, i.e., receive time. We used a plate model having vertices on 6° centers, which we found to be a suitable compromise between performance and fidelity. Fluxes were converted to generic magnitudes and the optimal offset to Rband was also estimated. Some individual batches of photometry also required the estimation of an independent, ad hoc magnitude offset, typically due to coma contamination or photometric calibration issues.

The least squares fitting process converged well when near a local minimum, but nonlinearities often led to large corrections when the initial guess was far from the minimum. Thus special care was needed in slowly building up to a global fit to larger data sets, *e.g.*, an entire quiescent period. A typical fitting approach was to estimate the spin state with a short (few to several days) but

relatively dense data set, where the light curve variation was clearly visible. The epoch t_0 would be situated within this data set (Fig. 12). Adding more and more data to slowly extend the fit span occasionally yielded good results, but in many cases the measurement gaps were too large to prevent ambiguities in the number of intervening rotations. An alternate method was to fix the rotation phase obtained from the short, dense data set and then scan a wide range of rotation rates to see which ones fit the larger data set the best. This approach yielded something akin to the periodograms used in the Tucson approach, but which had a somewhat different origin and interpretation (Fig. 13). With this approach we could generally identify a single or perhaps a few candidate frequencies that could be considered more carefully.

Overall, fits were generally acceptable, but as can be seen from Fig. 17, the model light curve did have a significant departure from the measured light curve. This was associated with illumination of regions where the shape model is not well constrained by the *Deep Impact* approach photometry. However, the fitting process need only fit the gross features of the light curve and so mismodeling of the light curve was not a serious obstacle to estimating the rotation state, aside from the 180° phase ambiguity discussed in Sec. 5.2 below.

Ground-based Photometry. This large data set, described more exhaustively by Meech *et al.* (2011), formed the foundation for all of the quiescent fits in Regions A, B, and C. Most of the photometry obtained while the comet was highly active was not usable for rotation estimation, but many good batches even with substantial coma contamination were found to be helpful. For

the JPL method, isolated individual observations contributed little to rotation knowledge, but the numerous batches (*e.g.*, Fig. 12) showing clear light curve variation and slope from night tonight proved to be vital.

Deep Impact Photometry. The densest set of photometry available for this study was that derived from the approach photometry from the Deep Impact mission. This data set followed the model light curve with excellent coverage over seven weeks (Fig. 14) and, moreover, it was obtained while the comet was active and the spin state was presumably accelerating. With this in mind, we extended our rotation model to estimate the angular acceleration of the comet during the Deep Impact approach and found that the comet was indeed spinning up during this time. The acceleration model applied a torque proportional to the sublimation rate of water, as given by the g(r) function commonly used to model nongravitational accelerations on comets (Marsden et al. 1973). This approach allows the acceleration to build slowly, reaching a peak at perihelion and then fading back to effectively zero around 2.5 AU post-perihelion. As we explain beow, the comet acceleration profile was rather more complex, but we were still able to use this simpler model to estimate the acceleration on the relatively short interval of the *Deep Impact* approach. Specifically, we find that the best-fitting acceleration according to this model is dS/dt = A * g(r), where $A = 0.0789\pm0.0031$ deg/day². Thus formal uncertainty is only about 4%, and so the estimated acceleration is non-zero with very strong statistical significance. This model indicates an acceleration starting at 0.024 deg/day² at the beginning of the Deep Impact data set and reaching 0.028 deg/day² by the end of the data set about a

day before perihelion. This model was eventually superseded by the acceleration profiles described in Sec. 6.

Hubble Space Telescope and Spitzer Photometry. Photometric observations of Tempel 1 taken by the Hubble Space Telescope were obtained in 1997 (Lamy et al. 2001, 2007) and 2009 (Meech et al. 2011) Each of these data sets proved crucial in establishing the spin state in Regions A, B, and C because of the dense coverage and high SNR that unambiguously showed the light curve morphology. Spitzer flux measurements (Lisse et al. 2005) were converted to magnitudes and compared with predictions for visible magnitudes. While we chose not to actually fit these data due to uncertainties about the relative shape and phasing of light curve extrema, we found that the placement of observed Spitzer extrema did agree well with that predicted for visible extrema.

5.2 The Tucson Method. The sidereal spin rates, S_j , are determined separately from the rotational phases, W_{0j} . They are determined without reference to *model* lightcurves and, to remove drift in the rotational phase of the observed light curve due to changes in the solar phase angle (Surdej and Surdej, 1978; Harris *et al.*, 1984) and orbital motion, the observing times are adjusted to create a data set for each region as it would have been observed by a fictitious observer viewing the comet from the direction of the ascending node of the comet at zero solar phase angle. After correcting for light time, this ensures that periodicities in the modified light curve reflect the sidereal spin of the nucleus. Because of changing sub-solar and sub-observer latitude at the elongated nucleus (Fig. 6) the shape

of the observed light curve will not be consistent in amplitude, but, because of the low obliquity of the comet (11.9°), this effect is expected to be small. We do expect, however, that it will introduce some amplitude dispersion in the rotationally phased light curves.

Once the Sj are determined, the rotational phase in each region is then estimated by comparing model light curve predictions, based on the Thomas shape model and a Hapke phase function, to high S/N *Hubble Space Telescope* data. In the case of Region A, where the Lamy *et al.* (2001) *HST* data do not cover a full rotation period, ground based data are also used in the determination of rotational phase.

Removal of synodic, solar phase angle, and light time effects. The observing time for a particular observation is first adjusted to zero solar phase angle using a variation of the Phase Angle Bisector (PAB) method of Harris *et al.* (1984). These authors note that as the solar phase angle increases from zero the rotational phase of the light curve drifts in the same direction but at approximately half the rate. Since the timescale for change in the solar phase angle, α , is much greater than the rotational period, the rotational phase $W_j(\alpha)$ of the observed light curve at solar phase angle α will be shifted by $\Delta W_j(\alpha) = \beta(\alpha/2)$ from its value at zero phase where β is the longitude interval between the meridian that passes through the sub-solar point and the meridian that includes the PAB. $\Delta W(\alpha)$ corresponds to a timing correction of $\Delta t(\alpha) \approx P^*\Delta W(\alpha)/360$ where P is the estimated rotation period. Using the same logic the timing correction for the orbital position of the comet at time, t, is $\Delta t(\gamma) \approx P^*\Delta W_s(\gamma)/360$ where γ is the

longitude interval between the meridian that contains the sub-solar point and the meridian that contains the ascending node. The total correction to the observing time is therefore $\Delta t = \Delta t(\alpha) + \Delta t(\gamma) + \Delta t(d)$ where $\Delta t(d)$ is the light time correction for an observer at a distance d from the nucleus. Δt varies considerably throughout the various observation sets and falls in the range of 0.81 > Δt > 0.20 d.

Preparation of the data for high precision frequency analysis. The data are first linearly detrended (this is a small correction as can be seen from Fig.11) and a preliminary value of S_j is determined with the ANOVA (ANalysis Of Variations; Schwarzenberg-Czerny, 1996) period-finding algorithm in the commercially available Peranso software package (this is available at www.CBABelgium.com). We experimented with the thirteen period finding routines, which include all of the major astronomical period-finding algorithms, in the Peranso package on various subsets of the data and found that the ANOVA algorithm gave the clearest and most consistent results. Other often-used methods, such as FALC (Harris et al., 1989) and PDM (Stellingwerf, 1978), gave effectively identical results.

We have used the uncertainty estimates as calculated in the *Peranso* package. The method used is that described by Schwarzenberg-Czerny (1991) in which the uncertainty in the period is taken as the width of the associated peak at the mean noise level down from the peak.

Once the preliminary period estimates have been calculated they are used to rotationally phase the data so that they can be examined to estimate bias corrections for particular observing runs and remove obviously discordant

outliers. In this way the data sets can be "cleaned-up." This process, removes small systematic photometric errors that may arise between groups of observations taken under different viewing conditions, with different photometric equipment, and under observing conditions of different clarity and seeing.

The cleaned-up data are then analyzed with the ANOVA algorithm a second time to obtain the final estimates of periodicities and uncertainties. This process yields our 'best' estimate of the period and its uncertainty in each observational region. While this two step process is not one that we would recommend for finding periodicities *ab initio* in an arbitrary data set, we have confidence in using it here because of the special knowledge produced by the *Deep Impact* encounter photometry. *I.e.*, we know the approximate spin period and have a fair idea of the shape of the light curve, knowledge that we use to discriminate against spurious period estimates. ANOVA periodograms and cleaned-up rotationally phased light curves and for the region A, B, C and the DI data are shown in Figs. 15, and 16 respectively.

Determination of rotational phases. To determine the rotational phase, W_{0j} , of the data in each observation region we have relied primarily on HST data, which, in regions B and C, provide consistent and well-sampled coverage over a complete rotational cycle. The phase is tied into the Thomas $et\ al.\ (2007)$ nucleus coordinated system by fitting the observed light curve to a model light curve computed from the Thomas $et\ al.$ shape model using the online tool noted earlier. The final fits to the data are shown in Fig. 17. The accuracy of fit is estimated at \pm 2° in rotational phase by visual inspection. A detailed examination of Fig. 17

shows that there is a distinct possibility of a 180° ambiguity in rotational phase. This shown more clearly in Fig. 18. We have used both numerical cross-correlation and visual inspection to decide the appropriate alignment of the model to the data. However, the results of both methods are, in our opinion, marginal. While both of these techniques support the choice of alignment that we advocate in this paper the possibility of a ~180° error in rotational phase must be entertained.

The fits in Figs. 17 show that the model is delinquent if the range of rotational phase associated with the primary minimum of the observed light curve and that there is a possible ambiguity of 180° in rotational phase. The final estimates for S_j and W_{0j} are collected in Table 2 and the evolution of S_j with time is shown in Fig. 18.

Direct determination of the acceleration of the spin rate. Because the comet was active during the collection of the *Deep Impact* data we recognized that it could contain direct information on the acceleration of 9P/Tempel 1's spin. We therefore applied the dynamical period estimation methods of Drahus and Waniak (2006), which simultaneously yield both a spin rate and its acceleration (assumed linear in this case) at the mid-time of the observations (Appendix B contains a detailed description of its application to the *Deep Impact* data). This yielded a period of 1.69961 ± 0.00023 d (211.814 ± 0.029 °/d) applicable at JD 2453530.60510 and a rate of change in the spin rate of $+0.020 \pm 0.003$ °/d/d. As can be seen in Fig. 18 this value is consistent with the period change through

perihelion that we have found in the Earth based data if the timescale over which the torque acts is ~63 days.

The JPL and Tucson approaches described here are substantially independent, and indeed complementary. Through the use of the light curve generation tool, the viewing geometry, phase angle correction and light time delay are automatically incorporated into the JPL estimate without the careful bookkeeping and modification of the time tags required for the Tucson method. However, because of its reliance on the light curve generation tool, and in particular the Thomas *et al.* shape model, which did not accurately model the light curve at some rotation angles, the JPL approach suffered from somewhat poor fits. This led to some irresolvable ambiguities in determining which frequency was correct. In contrast, the Tucson approach did not rely on light curve models, or any other model, to identify the best fitting rotation rate. In this sense the Tucson approach is more robust in determining the rotation rate, while the JPL method seamlessly revealed the rotation phase of the comet.

6. The dynamical evolution of the spin rate of 9P/Tempel 1

Tables 2 and 3 contain our best estimates of the overall spin state of 9P/Tempel 1 and the changes that occurred during the perihelion passages in 2000 and 2005. Table 3 focuses on spin rates and orientation of the polar axis while Table 2 gives information on rotational phase. The spin rates and acceleration in Table 3 are the average of the values found in the JPL and Tucson studies.

In Figure 18 we plot the observed spin rates and acceleration as a function of time. The spin rates derived from Earth-based measurements can be seen to systematically increase as the comet passes through succeeding perihelia in agreement with the sense, but not the slope, of acceleration that is derived from the *Deep Impact* photometry alone. Referring to the discussion in section 4 we assume that the changes in spin rate are the result of a smooth evolution of non-gravitational torques through perihelion and from perihelion to perihelion. The fact that the spin rate measured by *Deep Impact* is greater than that measured both before and after perihelion and that it is closer in value to that measured after perihelion suggests that non-gravitational torques are not symmetric about perihelion and that, for a part of the time, positive torques dominate while at other times the reverse is true. It seems clear that the dominant effects of non-gravitational torques occur well before perihelion passage.

The acceleration measured during *Deep Impact* approach allows us to compute the magnitude of the torques acting on the nucleus at that time and estimate the moment arm that was involved. Assuming a homogeneous mass distribution in the interior, a spherical approximation for the shape, and using the mass range determined by Richardson *et al.* (2007), we find that the moment of inertia of the nucleus lies between $0.8 - 4.6 \times 10^{19} \text{ kg.m}^2$. To achieve the observed spin rate acceleration implies that a torque of $0.3 - 2.5 \times 10^7 \text{ kg.m}^2 \cdot \text{s}^{-2}$ was acting on the nucleus. Jewitt (1997) has related the average torque to total mass loss in teRMS of a "dimensionless moment arm," k_T, for which he conjectured a value of ~0.05. With the measurements reported here we can now

make an *observational* estimate of k_T for 9P. Schleicher (2007) finds the production rate of OH to be ~ 7 x 10^{27} mol/s near the relevant time implying a water loss rate of only ~2 x 10^2 kg/s. Following Jewitt (1997) we assume a characteristic outflow velocity of 10^3 m/s and find $0.005 < k_T < 0.04$. This observational estimate is somewhat lower than Jewitt's conjecture but the result generally substantiates his approach.

The magnitude of the torque also permits us to say something about the stability of the pole direction. If we assume that there is a component of the torque acting at right angles to the spin axis for \sim 60 days (see section 5 above) we can estimate the angular displacement under forced precession during this time. The angular velocity of precession calculated this way is $\sim 1 \times 10^{-9} \, \text{rad.s}^{-1}$ and leads to a displacement angle of $\sim 0.3^{\circ}$ during perihelion passage. Unless the observed torque turns out to be a very small component of the total torque that is operating, which we think is unlikely, we expect that the pole direction of 9P/Tempel 1 should not precess more than \sim 1°/perihelion passage.

Modeling the evolution of the spin state. One of the objectives of this work is to predict the rotational state of the nucleus near the time of the *Stardust-NExT* encounter on Feb. 14, 2011. To do this a model of the non-gravitational torques is required. We have taken two approaches to develop such models – a *physical* approach, in which we attempt to emulate what we know the comets sublimation rates and jet structures, and an *analytic* approach that models the time behavior of torques with a prescribed functional form. As with the rotational analysis this modeling was done independently at both JPL and in Tucson with similar results.

Our physical modeling of torques was based on a heuristic 'rotating jet' model that has been used earlier to analyze the effects of non-gravitational forces on cometary orbits (Chesley and Yeomans, 2005) and in which the dependence of torque on heliocentric distance is prescribed by the function g(r) (Marsden et al., 1973). This sublimation "law" has had wide use in nongravitational force studies (Yeomans et al., 2004a). With this kind of model it is possible to match the spin rates and rotational phases of the nucleus across both the 2000 and 2005 perihelion passages; however, we also found that it was not possible to match the acceleration of the spin rate measured on *Deep Impact* approach at the same time. For this reason modeling based on jet torques was abandoned by both groups. An alternative physical approach is to consider torques associated with widespread sublimation of H₂O over the surface of the nucleus employing the Thomas et al. (2007) shape model. Such a study is already underway and Samarasinha (2010, private communication) reports that initial results indicate that model period changes through perihelion are somewhat similar to those measured in this work and that both phases of positive and negative net torque can occur during perihelion passage. Since this work was already in an advanced state we decided not to duplicate the effort and focused instead on analytic modeling. Since the analytic models produced at JPL and Tucson are quite different we present them separately. Even though the methods used by the two groups are quite different we shall find that they yield very similar descriptions of how the net torques currently operate during perihelion passage: on approach the spin rate first decreases, passes through a

minimum, and then accelerates rapidly through perihelion. After perihelion the spin rate goes through a maximum and then decreases to a stable level as the nucleus moves away from the sun.

The JPL torque model. Given the solutions detailed in Table 2 we can try to link together the various quiescent periods by examining the rotation phase runoffs induced by the torques encountered during the active intervals. We start with the 2005 perihelion passage since this case affords information on the comet's rotation state near the time of perihelion, as well as before and after. From fits to the *Deep Impact* approach data we know that the rotation phase W=219° on 2005 Jul 5.0 at perihelion. Meanwhile the pre- and post-perihelion quiescent solutions (Regions B and C in Table 2) predict W= 225° and W=104°, respectively, at perihelion. These imply that the accelerated comet gained 354° or -6° in rotational phase as it approached relative to a hypothetical unaccelerated comet. We call this the runoff. Similarly, but working in reverse time, the post-perihelion runoff is 245° relative to the unaccelerated post-perihelion solution. Thus according to these estimates the combined pre- and post-perihelion runoff is 239°(modulo 360°).

Using a similar approach at the 2000 perihelion, but without any active period constraints, we find that the combined runoff should have been about 208°, again modulo 360°.

We could not identify a torque profile that meets all of the constraints and leads to 354° runoff at perihelion, while we have developed an *ad hoc* model that

does lead to -6° runoff (Fig. 19). This model assumes piece-wise constant accelerations, and thus piece-wise linear spin rates. The key feature is that there is a modest (and so far not directly observed) deceleration before the dramatic acceleration seen in the *Deep Impact* data begins. This deceleration period would be about -0.0013 deg/day² and would start 400 days pre-perihelion and end 660 days post-perihelion, which corresponds well to the active periods seen in Fig. 4. Across this background deceleration is superimposed an acceleration of approximately 0.029 deg/day² that acts only for the 86 days before perihelion. This scheme would arise from a diffuse negative torque that acts for most of the active period and a single, strong, seasonal, jet-like active region that only acts for the three months prior to perihelion.

While this model is obviously crude and lacks a detailed physical basis, it does meet the observational constraints and serves one of the key purposes of the project, which is to predict the spin state of the comet at the epoch of the *Stardust-NExT* flyby in mid-February 2011. Here we can assume that the comet will essentially do the same as it did in 2005, or we can assume that there is some secular change and extrapolate from 2000 to 2005 to 2011. The former assumes implicitly that the perihelion-to-perihelion changes are best modeled as a random walk, while the latter would be most appropriate under the assumption that the comet is changing in a predictable way. Given the paucity of information we have about the variability of comet nucleus activity, each of these perspectives are equally defensible. For the present model we assume the random walk hypothesis and thus predict that the 2011 runoff will be -6° to

perihelion (2011 Jan 12.4). The additional 33 days from perihelion to the Stardust-NExT encounter (about 2011 Feb 15) should accumulate an additional 55° of runoff, amounting to a total of roughly 49°. The quiescent, post-2005 solution predicts W = 349° at 2011 Feb 15. Adding in the presumed runoff of 49° yields the accelerated prediction, W = 38°. The spin rate at that time should be 213.53°/day giving $W_0 = 172^\circ$ and, on 2011 Feb 15.0, the sub-solar longitude is calculated to be 328°. The mission target is W = 98° at closest approach and so we should delay the flyby by 60°, *i.e.* delay the encounter to 2011 Feb 15.28. This is a 10 hour delay from the nominal (*i.e.*, before February 2010) arrival time of 2011 Feb. 14.8625.

The Tucson or "Gauss" analytic model. Here we divide the component net torque, T(t), at time t in Eq. 4 into two parts, to give the model the flexibility to represent both negative torques and positive torques separately as follows:

$$T(t) = T_1 * \exp((t - t_{max1})/\tau_1)^2) + T_2 * \exp((t - t_{max2})/\tau_2)^2)$$
 (9)

The Gaussian shape assumed here is quite arbitrary and was chosen simply because it had the right *general* character for torques generated by sublimation and, more importantly, it allowed the integration for the spin rate to converge. The shape should be thought of as an interpolation function. We did experiment with Lorentzian shapes, but found that the extended wings gave unrealistic torques that extended too far into the region around aphelion.

The model therefore has six parameters, T_1 , T_2 , t_{max1} , t_{max2} , τ_1 , and τ_2 and, when applied to the 2005 perihelion passage, seven constraints – the observed spin rate and rotational phase at three times and the acceleration of the spin rate at a single time. A *MathCad* program was developed to solve Eq. 4 as a function of assumed values for the parameters t_{max1} , τ_1 , and τ_2 . Preliminary values for T_1 , T_2 and t_{max2} were first estimated using the three observed spin rates and the acceleration at *Deep Impact* encounter. Given the initial rotational phase in a torque free region, Eq. 6 could then be integrated to provide an estimate of the rotational phase spin rate at the time of the other two observations. The parameters t_{max1} , τ_1 , and τ_2 were then adjusted (by hand) in an iterative cycle until the model rotational phases agreed with the observed values to better than 1°.

At the 2000 perihelion we have only four constraints and it is not possible to solve for all of the parameters. We have therefore assumed that the parameters that depend primarily on the geometry of the perihelion passage, t_{max1} , t_{max2} , τ_1 , and τ_2 , have the same values as in 2005. We expect this to be a reasonable assumption providing that any precession of the spin pole (or the orbit) is, as we have assumed, negligible. In this way it is possible to calculate appropriate values of T_1 and T_2 for the 2000 perihelion passage.

The results of these calculations are collected in Table 4 and the torque profile and spin rate evolution for the 2005 perihelion passage are shown in Figure 20. We see that the observations, as expected, require T_1 and T_2 to have opposite signs. The predicted net torque profile initially moves to a negative value before achieving a positive maximum some 32 days before perihelion. In

addition, as expected from the decrease in the amount of period change through the 2005 perihelion relative to that at the 2000 perihelion, the magnitudes of the model torques are also seen to decrease from 2000 to 2005.

We use the parameters determined at the 2000 and 2005 perihelion passages to predict what the torque profiles may look like in the 2011 perihelion passage. First, we again assume that the parameters that depend primarily on geometry remain the same in 2011 as in 2005. Second we linearly extrapolate the values of T_1 and T_2 found in 2000 and 2005 to 2011. The resulting values of the T_1 and T_2 are shown in Table 4 and the predicted spin rate profile for 2011 in Figure 21. Putting these three solutions together we can plot our estimate for the complex evolution of the spin rate throughout the period 1997 – 2010 and the prediction for 2011. This is done in Figure 22.

7. Discussion and predictions for Stardust-NExT encounter

The observations collected during the *Deep Impact* World-wide campaign cover an interval of thirteen years and two perihelion passages and clearly imply (Fig. 18) a roughly "stepwise" increase of the spin rate of 9P/Tempel 1 as the comet passes through succeeding perihelia. In addition, most of the torque must have been applied well before perihelion. The spin rate and its acceleration measured from the *Deep Impact* approach photometry imply even greater complexity in requiring that phases of both positive and negative net torque operate through the observed perihelion passages. The observations and modeling appear to support the idea that the torque producing outflow is dominated by the

sublimation of H₂O over a large fraction of the surface of the nucleus and is a result of its shape. Modeling indicates that the production of net torque is unlikely to be dominated by observed jet structures except, possibly, in the period just before perihelion passage. While the spin pole direction is certain to precess as a result of these torques, the rate is expected to be small, < 1°/perihelion passage. If it becomes possible to measure the displacement of the direction of the spin pole at the *Stardust-NExT* encounter in 2011 we should be able to deduce more about the distribution of the outflow with respect the surface of the Thomas *et al.* (2007) shape model.

Relationship to the water production rate. Observations of OH production by Osip et al. (1992), Schleicher (2007), and Cochrane et al (2009) and, in particular, their interpretation by Schleicher, indicate that the water production rate peaks 30 - 60 d before perihelion and has moved closer to perihelion by 5-10 d between the 1983 and 2005 perihelion passages. Apportioning this change equally among the intervening perihelia this gives roughly a shift of 1 – 3 d/perihelion. In addition, the production rate decreased by 42% between 1983 and 2005.

These changes are qualitatively consistent with the present observations in that the period change, and therefore the implied production rate of the operating outflow, decreased between 2000 and 2005. Also the (model) torque peaks well before perihelion (32 d) as does the observed H₂O production rate. The H₂O production rate implied by the model at the peak torque fell by 5% between 2000 and 2005.

Our observations and analytic modeling do not provide a quantitative explanation for the shift of the H_2O production peak by 1-3 d/perihelion passage. But we presume that this is the result of small changes in the distribution of sublimation over the nucleus surface from perihelion to perihelion or, possibly, slow precession of the spin axis.

Predictions for the Stardust-NExT encounter with 9P/Tempel 1. The primary objective of the mission is to see what changes occurred on the regions of the surface previously imaged in the *Deep Impact* mission as a result of the activity during a single perihelion passage and, secondarily, to characterize the artificial crater formed by the impactor spacecraft. In January, 2010, when timeof-arrival trajectory maneuvers were being planned, the spacecraft was projected to arrive at the comet on UT 2011, February 14 at 20:42:34.8 (JD 2455607.36290) some 34 d after perihelion passage. To have the best chances of accomplishing these objectives the spacecraft should arrive at encounter when at least 25% of these regions and the crater are in daylight and visible to the spacecraft camera system. Figure 23 is a contour plot which shows the encounter conditions that must prevail in order to achieve the above objectives. By providing a time-of-arrival (which sets the sub-solar longitude at encounter time) and a spacecraft B-plane angle that avoids the dark blue area it is possible to ensure that the mission will achieve its objective.

In the JPL study, in order to make a prediction for the spin state at Stardust-NExT encounter, the spin evolution model that was developed for the 2005 perihelion passage was simply transferred to the 2011 time frame by modifying the initial spin rate and rotational phase to that appropriate for region C. This approach was based on the assumption that changes in the torque profile from perihelion to perihelion cannot be easily predicted and that the comet is likely to behave at one perihelion essentially as it did at the previous perihelion. This yielded a spin rate of 213.52 °/d and a sub-solar longitude of 328°W at encounter on UT 2011 Feb 15.0 (299°W on Feb 14 20:40).

In the Tucson study, the value of the parameters T₁ and T₂ in the Gauss model that are appropriate for the 2011 perihelion passage are obtained by a linear extrapolation of their values in 2000 and 2005. The values of the other parameters in the Gauss model are, as explained earlier, taken as the same as in 2005. The model yields a spin rate of 213.47 °/d, $W_0 = 15.9$ °, and a sub-solar longitude of 242 W on 2011 Feb 14 20:40. The two models differ by 57° in their prediction of sub-solar longitude. In order to be specific, and since the two results are reasonably close (i.e., both well within a single quadrant), we simply take their average as our final estimate for the sub-solar longitude at nominal encounter and treat the difference an indicator of the level of uncertainty in the result, i.e., we take the sub-solar longitude at the nominal time of encounter (UT 2011 Feb 14 20:40) to be 271 ± 29° W. This result is plotted on Figure 23 as a black dot and bar and shows that a trajectory correction maneuver to delay the time of arrival by at least 8h is needed to be sure of attaining the primary science objective. In Figure 24 we show, using the Thomas et al. (2007) shape model, the predicted aspect of the nucleus as seen from the Stardust-NExT spacecraft

at the nominal encounter time (LHS) and the case where the encounter time has been delayed by 8h (RHS) where there is not only ample *Deep Impact* terrain to observe but also what should be a spectacular view of the artificial crater. A burn to accomplish a ~8h delay in arrival time (the maximum allowed by the available fuel) was performed in February, 2010.

Finally, we note that there is an important caveat to the above prediction: there is, as noted in section 5, the possibility of an error of 180° in the predicted rotational phase. If this is the case then the nominal encounter time will achieve excellent viewing of *Deep Impact* terrain at a sub-solar longitude of ~91° W without a trajectory correction maneuver. With a time delay of 8 h, implementing the trajectory correction moves the sub-solar longitude at encounter to ~162±25° W. As can be seen from Figure 23 this still allows the possibility that the primary science objective will be achieved, but that imaging of the artificial crater would be unlikely.

8. Conclusions.

In this paper we have provided a detailed analysis of light curve information from the *Deep Impact* World-wide observing campaign and data obtained from the *Hubble* and *Spitzer Space Telescope*s and the *Deep Impact* mission that were obtained between 1997 and 2009. This analysis shows:

1. The spin rates (periods) changed in an approximately stepwise manner through the 2000 and 2005 perihelion passages. From 209.023 \pm 0.025 °/d (1.7223 \pm 0.0002 d) prior to 2000 to 210.448 \pm 0.016 °/d (1.7106 \pm 0.0001

- d) between 2000 and 2005 and then to 211.814±0.029 °/d (1.6996 ± 0.0002 d) during the *Deep Impact* approach to 211.625±0.012 °/d (1.7011 ± 0.0001 d) post-2005.
- 2. The period shortened by 16.8 ± 0.3 min during the 2000 perihelion passage and by 13.8 ± 0.2 min during the 2005 perihelion passage.
- 3. The angular acceleration was 0.024 ± 0.003 °/d² during the *Deep Impact* approach.
- In 2005 the angular acceleration was not symmetric about perihelion and most occurred well before perihelion passage.
- 5. Sublimation outflow of H₂O over most of the surface of the elongated nucleus with a possible contribution from jet activity just prior to perihelion are likely the causes of the torque.
- The level of torque required to explain the *Deep Impact* observations suggests that precession of the spin axis is small, *i.e.*, < 1°/perihelion passage.
- 7. The trend in the net change of spin rate through the two perihelion passages is in a direction expected from the published trend in H₂O production rates observed at the 1983 through 2005 perihelia.
- 8. The observed peak in H₂O production rate some 30 60 days before perihelion is in concert with the predicted peak in torque at 32d before perihelion. The H₂O production rate implied by the Tucson torque model fell by 5% between the 2000 and 2005 perihelia.

9. Analytic models have been used to predict the rotational state at the comet at the planned *Stardust-NExT* mission encounter in 2011. On UT Feb 14, 2010 20:40, the nominal encounter time in January, 2010, we predict that the sub-solar longitude on the nucleus will be 271 ± 29° West longitude (the average of the JPL (299°W) and Tucson (242°W) determinations). The spin rate is predicted to be 213.5 ± 0.2°/d.

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Table 1:The data used in the rotational analysis

Region	Number of	Time span	Standard	Heliocentric ²	Dates
	observations	(days)	deviation ¹	range (AU)	
Α	307	600	±11	4.5 - 2.2	11/23/97-7/15/99
В	541	1000	±12	4.1 - 3.5	8/16/01-5/11/04
DI	2888	50	±23	1.6 – 1.5	5/15/05-7/3/05
С	1074	1194	±13	3.6 - 3.3	9/24/06-12/30/09

¹ In brightness units; the mean nucleus brightness = 100 units. The large standard deviation in the *Deep Impact* data is due to noise from the coma that was present in the signal. ² For regions A, B, C the heliocentric range passes through aphelion at 4.74 AU.

Table 2:

Results of rotational analysis: Values of $W(t)_j = W_{0j} + S_j^*\Delta t$ for each region. *Units:* W_{0j} are in degrees, S_j are in °/d, and dS_{Dl}/dt is in deg/d/d. $\Delta t = (t(JD) - 2451545.0)$; ¹The JPL study assumed the Tucson value for S_A was correct. The spin rates for the *Deep Impact* data are given for the case of zero acceleration. When evaluating the values of W_{0j} between the two studies note that part of the difference is due errors in S_j propagating back to the reference time. The intrinsic lightcurve fitting error in W_{0j} (~ \pm 2°) is therefore much less than the differences would imply. Formal errors are given in the text.

JPL method	Tucson method			
$W(t)_A = 69 + 209.023 \pm 0.025^{1*} \Delta t$	$W(t)_A = 72 + 209.023 \pm 0.025^* \Delta t$			
$W(t)_B = 289 + 210.438 \pm 0.0xx^*\Delta t$	$W(t)_B = 280 + 210.458 \pm 0.016 * \Delta t$			
$W(t)_{DI} = 255 + 211.849 \pm 0.0xx^*\Delta t$	$W(t)_{DI} = 299 + 211.862 \pm 0.030^* \Delta t$			
$W(t)_C = 299 + 211.626 \pm 0.0xx^*\Delta t$	$W(t)_C = 301 + 211.623 \pm 0.010^* \Delta t$			
dS _{DI} /dt = 0.024 - 0.028	$dS_{DI}/dt = 0.020 \pm 0.003$			

Table 3.

The observed spin state of 9P/Tempel 1 and its changes through two perihelion passages (CY 2000 and 2005). * This estimate includes the effect of acceleration (assumed linear) during *Deep Impact* (DI) approach. [†] This estimate assumes zero acceleration in the spin rate during *Deep Impact* (DI) approach. Information on rotational phase is included in Table 2.

Orientation and sense of rotation	References				
Sense of spin		Thomas et al. (2007)			
Direction of pole (Positive or		Thomas et al. (2007)			
North)	(± 5° on the sky; J2000)				
Motion of the pole	Precession possi	Yeomans et al. (2004b);			
	< 1º/perihelion pas	Schleicher (2007); This			
	(Sh	(Short Axis Mode) state of rotation.			
	<u> </u>		1		
Rotation rates:	Epoch (days) (JD -2450000)	Period (days)	Angular rate (°/day)		
Pre - 2000	1224.88	1.7223 ± 0.0002	209.023 ± 0.025	This paper	
2001 - 2004	2477.37	1.7106 ± 0.0001	210.448 ± 0.016	This paper	
Deep Impact Approach*	3530.60	1.6996 ± 0.0002	211.814 ± 0.029	This paper	
Deep Impact Approach ⁺	3544.50	1.6993 ± 0.0002	211.856 ± 0.030	This paper	
Post - 2005	4297.00	1.7011 ± 0.0001	211.625 ± 0.012	This paper	
Rotational acceleration:		dP/dt (days/day)	dω/dt (deg/day²)		
Deep Impact approach	3530.60	$-1.9 \pm 0.1 \times 10^{-4}$	0.024±0.001	This paper	
Net change in rotation:	1	ΔP(minutes)	Δω(°/day)	_	
2000 perihelion passage 1546.13		-16.8 ± 0.3	1.425 ± 0.030	This paper	
2005 perihelion passage	3556.82	-13.7 ± 0.2	1.177 ± 0.020	This paper	

Table 4. Parameters for the Tucson "Gauss" torque model. The parameters are defined in Eq. 9. Details of the fitting process to the 2005 and 2000 perihelion spin rate and acceleration data is described in the text. The units of T_1 and T_2 are °/d/d.

Perihelion	T ₁	T ₂	T ₁ (d)	т ₂ (d)	t _{max1} (d)	t _{max2} (d)
2000	-0.112612	0.132565	180	159	-16.9	-22
2005	-0.110612	0.129355	180	159	-16.9	-22
2011	-0.108612	0.126145	180	159	-16.9	-22

Appendix A:

Description of the *Deep Impact* MRI Photometric Reductions (Contributed by Fabienne A. Bastien)

Photometric measurements of comet 9P/Tempel 1 were performed on images taken with the Medium Resolution Instrument on the *Deep Impact* spacecraft during the approach phase from 1 May 2005 to approximately 6 hours before impact on 4 July 2005. The MRI is a 12 cm aperture Cassegrain telescope with a 2.1 m focal length. Images were taken through clear filters that have a center wavelength of 650 nm and are uncoated and not band limited (Hampton *et al.*, 2005).

A total of 3014 images were analyzed: 595 science images and 2419 optical navigation images. The measurements were based on circular apertures ranging from 5 to 30 pixels in diameter with nucleus at the center of the aperture. The data consist of science images taken with the clear 1 and clear 6 filters and optical navigation images taken with the clear 1 filter. In the following discussion the images are displayed with lines increasing up and with samples to the right. Figure A1 (taken from Klaasen *et al.*, 2008) shows a full frame image with the quadrant nomenclature used below.

Properties of the Science data: Photometric measurements were made from the reversibly calibrated ("RADREV") science images. These images have had the standard pipeline corrections applied to them: bias and dark frame subtraction,

flat-field corrections, etc. They have not, however, been "cleaned" to remove artifacts such as cosmic rays. All images were taken in one of two sub-frame modes: 256x256 pixels for most of the approach sequence, and 512x512 pixels for the last 1.7 days of approach. The images display a number of problems not accounted for in the standard reduction. All images were affected by a horizontal striping of a few DN in amplitude caused by electrical interference. Additionally, the bias levels for these images are only known to the nearest full DN, and the bias level for each quadrant is different. Not correcting the images for this interference and, more importantly, for the imprecise bias subtraction can introduce systematic errors in the photometry in which the early approach images are primarily affected.

A further problem concerns the pixels in the two rows surrounding the horizontal boundary between the upper and lower halves of the CCD that are each 1/6 of a pixel smaller than the other pixels of the CCD due to the way the readout clocking was designed. This increases the point spread function of objects that overlap this boundary by 1/3 of a pixel. Flux measurements therefore tend to be greater at the boundary because the flat fielding during the pipeline processing assumes that all pixels are the same size. In approximately 80% of the images, the centroid of the nucleus lies within 20 pixels of this region; images taken through the clear 6 filter are particularly affected. Thus, most of the photometric measurements need to be corrected for this effect.

Properties of the navigation data. The raw optical navigation images are in a different format from the science images. Each image consists of a number of

square "snippets", each less than 400x400 pixels in size. Each "snippet" is centered on an object deemed interesting by the navigation team, usually a star or 9P/Tempel 1. Each set of snippets is integrated into a single image that is 1008x1008 pixels in size; the navigation data have neither serial-overclock nor parallel-overclock pixels. Therefore, quadrant bias must be determined via other methods. For a more detailed description of the navigation data, please see the Deep Impact Navigation Images Report included in the Deep Impact documentation data set, DI-C-HRII/HRIV/MRI/ITS-6-DOC-SET-V1.0, which is archived by the Planetary Data System.

Optical navigation data suffers from the same striping noise as the science data. However, because these data are in a different format from the science data, a different algorithm had to be applied to correct it. This procedure was also used to remove the bias. For the navigation data, the centroid position of the comet was sufficiently far away from the horizontal boundary between the upper and lower halves of the CCD (more than 30 pixels, on average) so that the photometric measurements were not affected by the smaller size of the pixels there.

Photometric reduction of the science data. The general procedure for the analysis of the science data is as follows: We start with RADREV calibrated data and then remove the horizontal striping. We then convert the data back to DN/s and perform the aperture photometry. These data are then corrected for the quadrant boundary effect (where needed). In order to remove the horizontal striping, the image is first divided into two halves: quadrants B and D to one side

and quadrants A and C to the other. The process is similar for each half: a region is defined, avoiding the overclock pixels, which will be used to determine the background. This is a two-dimensional array 25 pixels wide and whose length depends on the size of the image (256 pixels or 512 pixels). We take a resistant mean across each row of this array and store into a new array that is 1 pixel wide and 256 pixels or 512 pixels long. This then subtracted from each column of the half-image. Once the background noise is removed, circular aperture photometry is performed with apertures ranging in size from 5 pixels to 30 pixels in diameter. If the aperture falls across the boundary between the upper and lower halves of the CCD, the following procedure is used to correct the flux: We create a subimage centered on the comet that is slightly larger than the aperture. This subimage is then divided into two parts: part 1 is the portion of the image located above the quadrant boundary and part 2 corresponds to the part below the boundary. We measure the flux contained within the original aperture (i.e. with the center of the aperture at the original centroid position) that is in part 1. The centroid of the aperture is then shifted up by 1/6 of a pixel, and the flux remeasured. The difference between these two measurements is half of the necessary correction to be added to the total flux. The procedure is repeated for part 2, only this time the centroid of the aperture is shifted down by 1/6 of a pixel. Finally, we take the two central rows of the CCD (rows 511 and 512), and measure the flux from these two rows that contained within the aperture. One third of this value is subtracted from the total flux. Figure A3 illustrates this procedure.

Photometric reduction of the navigation data: The process is similar to that used for the science images except that the correction for the quadrant boundary is not applied. The background removal algorithm that we apply to the navigation images differs from that used for the science images in that the edge of the relevant snippet is used estimate the background instead of the edge of the image. Since the apertures used do not cross quadrant boundaries, it is only necessary to use one edge of the snippet. This procedure simultaneously determines the value of the background in the snippet and the bias.

Unfortunately this procedure does not work for images that were taken during the last week of approach. At this point, the comet's coma contaminates the entire snippet centered on the comet, and rarely are there any other snippets within the same quadrant (this is always quadrant D during this time period). In this case the value of the background is measured from the raw science images taken closest in time to the navigation image under consideration. A slightly different bias value is subtracted from the navigation images (358.5 DN) than from the science images (359 DN); however since the bias values applied to the science data are only determined to the nearest full DN, these two numbers are consistent with one another. Note that horizontal striping is not removed from images taken during this time frame. At this point in the sequence the comet is bright enough for the effect to be negligible. In 12 cases the comet was close enough to the quadrant boundary to require correction to the flux. Since these images comprise less than 0.5% of the total number of navigation images, these data were simply omitted from the analysis.

Appendix B

Investigation of *Deep Impact* photometry with the dynamical techniques.

Contributed by Michal Drahus

Deep Impact approach photometry (Section 3) was obtained close to perihelion, when the comet was active – thus providing an opportunity to seek angular acceleration in this data set alone. This would manifest itself as a small deviation from the constant periodicity. We performed such an analysis using the dynamical techniques introduced by Drahus & Waniak (2006).

We used their dynamical implementations of two classical algorithms: the Phase Dispersion Minimization (PDM), introduced by Stellingwerf (1978) and later improved by Drahus & Waniak (2006) to weight input data points according to their errors (which they called DPDM), and a Least Squares fit (hereafter harmonics fit) of a sum of harmonics, which also weights the input data. Both methods return a variance ratio R, which is a function of the rotation frequency ω_0 and acceleration $d\omega/dt$, and whose minima indicate the best dynamical solutions. Although the techniques allow for any *a-priori* law controlling the accelerating torque, in our analysis we assumed it was constant. This implies a constant $d\omega/dt$ and a linear evolution of ω with time. When the frequency is labelled with index zero, it refers to a specific moment of time t_0 ; throughout this section t_0 is the middle moment of the DI data set, which is June 9, 2005, 2:31:20.6 UT (JD2453530.60510).

Discovery of the secular spin-up of Tempel 1 made it possible to predict the frequency ω_0 and acceleration $d\omega/dt$ for the moment t_0 , and consequently to limit our analysis to the vicinity of the expected solution. Hence we investigated ω_0 between 0.024 and 0.025 h⁻¹ (which corresponds to the periods P_0 between 1.667 and 1.736 d), and $d\omega/dt$ between -5.0 and +5.0 × 10⁻⁷ h⁻². The DPDM was used with 20 to 200 bins (and always 5 covers), and the harmonics fit with 3 to 7 harmonics (including the base sinusoid). However, the results were found to be very weakly dependent on the settings. For the sake of clarity we present the solutions from the DPDM with 60 bins and from the harmonics fit with 5 harmonics (Fig. B1), and adopt their mean value as the final dynamical solution. The solution is $\omega_0 = 0.0245155 \pm 0.0000033 \text{ h}^{-1}$ ($P_0 = 1.69961 \pm 0.00023 \text{ d}$) and $d\omega/dt = +0.97 \pm 0.15 \times 10^{-7} \text{ h}^{-2}$, which unambiguously confiRMS slow spin-up of the nucleus. The parameters are significantly correlated, with the correlation coefficient of -0.70, which is a consequence of non-uniform distribution of the input data points. Note, that although data phasing is influenced simultaneously by ω_0 and $d\omega/dt$, for uniformly distributed points analysed with respect to the middle moment t_0 , the correlation would be weak or completely removed. Errors and the correlation coefficient were estimated following the Monte-Carlo approach of Drahus & Waniak (2006). We take as the noiseless reference light curve the harmonics fit with 5 harmonics, calculated separately for the solutions from both methods, we simulated 1000 realizations of noise for each of them, and determined the covariance matrices. Consequently, the mean matrix provided the errors and the correlation coefficient for the mean solution. It is

worth noticing, that the dispersion of both individual solutions about the mean is only 15% of the error in frequency and 56% of the error in acceleration, which shows an excellent consistency of both algorithms and suggests that uncertainties are reliably estimated.

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Figure captions

Figure 1. 9P/Tempel 1 R(1,1,α) magnitudes for 1997 through 2010 from the data of Meech *et al.* (2011) and Lamy *et al.* (2001, 2007). The ground based data are filled circles and the *HST* data are in red. The data set contains a subset of published V magnitudes that have been converted to R using (V-R) = 0.50. The short black vertical lines show the times of opposition and the dashed vertical lines denote the time of perihelion passage. The horizontal orange bars show the range of data in each region that is used in the rotational analysis. Note how the comet brightens as the solar phase angle decreases near opposition.

Figure 2. Phase laws. The R(1,1, α) data (black dots) with various phase functions proposed for 9P/Tempel 1. Shown are the integrated phase function of Li *et al* (2007) (dotted line), the phase law polynomial of Belton *et al* (2005) (dashed line), and a linear correlation to the data (continuous line). We use the latter (R(1,1, α) = 14.905 + 0.0449 α) to correct the magnitudes to zero phase angle (α).

Figure 3. R(1,1,0) versus calendar year. The magnitude data has been corrected to zero phase angle using a linear phase law of 0.0449α mag/deg. The flat trend around the time of each aphelion passage indicates that coma there is negligible and the scatter in that region is almost entirely due to the spin of

the nucleus. The red circles denote HST data. The horizontal orange bars shows the range of data in each region that was used in the rotational analysis.

Figure 4. R(1,1,0) versus time from perihelion passage. The filled points are relative to the Jan 2, 2000, perihelion passage and the open circles are relative to the July 5, 2005, perihelion passage. The open triangles were taken in the fall of 2008 and refer to the 2011 perihelion. This figure shows the repeatability of the data from one perihelion to the next and also the asymmetry of the light curve about perihelion (see also Figure 5).

Figure 5. R(1,1,0) versus heliocentric distance. The brightness asymmetry about perihelion is clearly evident. The filled points are pre-perihelion, the open circles are post-perihelion. Notice that the mean trend becomes independent of heliocentric distance beyond 4 AU, indicating that light scattered from the nucleus dominates the signal.

Figure 6. Sub-solar (solid line) and sub-earth (dashed line) latitudes (left ordinate) for 9P/Tempel 1 from 1997 to 2011. The data, $R(1,1,\alpha)$, are also shown (right ordinate). The sub-earth latitude varies from -5 deg at the 2002 opposition to -14 deg at the 2004 opposition and this change of viewing geometry has an effect on the shape of the light curve. The increase in sub-earth and sun latitudes from negative to positive latitudes just prior to

perihelion passage is important in the interpretation of H₂O productions rates (Schleicher, 2007) and consequently the torques on the nucleus (see Section 6).

Figure 7. The orbits of 9P/Tempel 1 and the Earth projected onto the ecliptic (since the comet inclination is low, its true orbit rises above the plane of the figure by, at most, 0.482 AU). Shown are the directions of the comet from the sun at each opposition covered by the data. The wide spread of these directions shows why timing corrections must be made to the observations if the data from different oppositions are to be phased together and a sidereal rotation period determined. Also shown (dashed line) is the projection of the direction from the ascending node of the nucleus equatorial system (λ = 202.03, β = 9.24) toward the nucleus that is used as a basic reference direction when making corrections for synodic and illumination effects.

Figure 8. Fraction of signal due to the nucleus in each data point of the *Deep Impact* approach photometry. Evidently coma dominates the photometric signal for most of the data until about 4 days before impact (see text for a detailed explanation).

Figure 9. *Deep Impact* approach photometry. The top two panels show a normalized version of the science and navigation data separately after the clean-up process that removed variability due to mini-outbursts (Farnham *et*

al., 2007; Belton et al., 2008). The data, in 'data numbers' (DN), are normalized by the factor $r^2d^2/C_nf(\alpha)$ as described in the text. Also shown are 4^{th} -order, least-square fit, polynomials fitted to the data. These represent the general run of the sum of the underlying coma signal and the mean nucleus signal. In the lower panel is the difference between the data and the polynomials, which is taken to represent the rotational variability of the nucleus.

Figure 10. Plots of post- and pre- 2005 perihelion brightness in relative brightness units (mean nucleus brightness = 100 units) after the mean brightness of the nucleus has been removed. The dashed horizontal lines show the mean brightness of the nucleus for comparison purposes. These plots make it easy to evaluate the relative contributions of the coma and nucleus to the total brightness and determine the heliocentric distances between which the production of a coma is insignificant, *i.e.*, from 4.1 AU post-perihelion to 3.2 AU pre-perihelion. The curves are polynomials, which, as can seen, only approximately represent the run of the coma levels. They are not used in the analysis and are shown only to indicate the general trend of coma brightness.

Figure 11. Brightness data for 9P/Tempel 1 used in the rotational analysis. The data are shown after the clean-up process (see text) and displayed as a function of observing time. The three observing regions defined in Figure 1

- are shown separately. The mean brightness of the nucleus (100 units) has been removed.
- Figure 12 An example of the fit of data in the JPL analysis over a limited interval around an assumed t₀ (in this case in Region A) to the predicted model light curve (black line).
- Figure 13 An example of an alternate method to determine the spin rate used in the JPL analysis where the RMS of residuals are minimized over fits to a short, dense, data sample over a range of assumed spin rates (ω).
- Figure 14 Model light curve fits to the *Deep Impact* approach photometry in the JPL analysis. The dark black line is for the Hapke phase function. The colors of the data points represent different regions of the fit that were used to estimate the acceleration of the spin rate.
- Figure 15 ANOVA periodograms for the data in Figs. 9 and 11.
- Figure 16 The cleaned-up data for each observation region phased with the spin rates in Table 3.
- Figure 17 Fits of model light curves to the *HST* data that determine the rotational phase in each observation region. In the top two panels we show the preferred fit based on numerical cross-correlation and visual inspection. Both of these methods give only marginal assurance of the best fit (*i.e.*, a 180° ambiguity is possible). Note the discrepancy in the fit near the primary minimum in both sets of data. In the bottom two panels we show the fit of the model to a combination of Region A *HST* and ground-based data again illustrating the possibility of a 180° ambiguity.

Figure 18. Spin rate results for 9P/Tempel 1. The black points are the spin rates deduced from the data in regions A, B, *Deep Impact*, and C and listed in Table 3. The dashed line indicates the slope determined from the *Deep Impact* approach photometry. The horizontal red lines show the time period covered by the data in each region that was used to estimate the spin rate. The *predicted* spin rate (212.522 ± 0.174 °/d) near aphelion following the 2011 *Stardust-NExT* encounter is shown in aqua. The observational error associated with the observed points is smaller than the dots; the error in the predicted point is a formal 1σ error based on an extrapolation from the observations taken around the 2000 and 2005 perihelia. The vertical dashed lines in red show where the perihelia of 2000, 2005 and 2011 fall.

Figure 19. JPL torque model. Bold dashed segments depict constraints obtained from photometric fits, before, during and after the 2005 perihelion passage.

Area of triangles are A= -74°, B= 68°, C= 245°. Area of rectangle D is ~55°.

Area A+B+D=49° is the estimate of the rotation runoff from the pre-perihelion, quiescent solution (Region B) at the epoch 31 days after perihelion, which corresponds to the *Stardust-NExT* flyby.

Figure 20. Fit of the "Gauss" torque model to spin rate and rotational phase data spanning the 2005 perihelion and including the *Deep Impact* results. (*Top panel*) The component torques (green and blue) and the net torque (red) scaled to unit moment of inertia as a function of time. Note that the net torque is predicted to maximize 32 days before perihelion passage (red dot-dash vertical line). The net torque is at first negative and then rises to a positive

maximum. The torque falls off becoming negative again before fading out. The bulk of the torque operates for ~ 300 days around perihelion. (*Bottom panel*) The modeled run of spin rate in the vicinity of perihelion. The observed spin rates are marked in blue and lie precisely on the model curve. In addition the rotational phase at each point is reproduced to within ~1°. The rate of change of the spin rate measured from the *Deep Impact* approach photometry is shown as an inclined dot-dash line. In this model the predicted slope near perihelion is not precisely satisfied with the predicted value ~ 10% less than the measured value.

Figure 21. The spin rates predicted by the "Gauss" model around the 2011 perihelion including the time of the *Stardust-NExT* encounter (Feb 14, 2011). The time of encounter is shown as a black dot-dash vertical line. The only measured spin rate in this figure is that at JD2455074 the other two are predictions. The spin rate at encounter is estimated as 213.47 °/d. See text for details of the prediction. The time of perihelion is denoted with a vertical dotted green line.

Figure 22. Modeled evolution of the spin rate of 9P/Tempel 1 through three perihelion passages. The dashed blue line is the Gauss (*see text*), non-gravitational, torque model fit to the 2001-2004, *Deep Impact*, and post-2005 spin rates and rotational phases. The predicted evolution of the spin rate through the encounter of the *Stardust-NExT* mission on Feb 14, 2011, is also shown. The black points are the spin rates deduced from the data in regions A,B, *Deep Impact*, and C that are listed in Table 2. The dashed line indicates

the slope determined from the *Deep Impact* approach photometry. The *predicted* spin rates at encounter on Feb 14, 2011 (213.47 °/d) and near aphelion (212.52 °/d) following the 2011 encounter are also shown. The vertical dashed lines in red show where the perihelia of 2000, 2005 and 2011 fall.

Figure 23. Contour plot of the percentage of the 2005 *Deep Impact* imaging coverage that will be observable at Stardust-NExT encounter as a function of sub-solar longitude at the time-of-arrival and the spacecraft B-plane angle with respect to the sun-line. The blue area is <25%, the magenta area achieves 25-50%, the yellow area achieves 50-75%, and the grey area achieves 75-100%. The green dot denotes the arrival conditions for optimal viewing of the *Deep Impact* crater. The black dot and bar denotes the conditions for the nominal time-of-arrival on Feb 14, 2011 20:42 given the predictions based on the observations analyzed here. Since it falls in the blue region of the plot the Level 1 NASA requirement of imaging at least 25% of the Deep impact coverage is unlikely to be attained without an adjustment of the time-of-arrival. A time-of-arrival adjustment of a delay of ~8 hr is required to move the black point and its estimated error into the magenta area and achieve the requirement. Such an adjustment was made by a trajectory correction maneuver in February, 2010.

Figure 24. The anticipated view of the nucleus of 9P/Tempel 1 from the *Stardust-NExT* spacecraft at closest approach on a trajectory that has the subspacecraft latitude at -11°. Grey represents areas previously imaged by *Deep*

Impact while blue is terra incognita. Also shown is the position of the Deep Impact crater, the prime meridian, and the position of the South pole. The LH panel shows the view with the nominal time-of-arrival in January 2010; The RH panel shows the view with the maximum 8h delay in the time-of arrival.

Figure A1. A full frame MRI image showing the quadrant nomenclature.

Figure A2: Illustration of the procedure used to create a uniform background in the MRI science images.

Figure A3: Procedure used to correct comet flux measurements for the quadrant boundary effect (see text). The cross at the center of the aperture corresponds to the comet's centroid position. The green line represents the quadrant boundary. The correction consists of subtracting 1/3 of the flux from the rows at the boundary. The yellow shaded areas illustrate what is added back in.

Figure B1. Dynamical periodograms calculated with the methods of Drahus and Waniak (2006) showing the variance, R, in the *Deep Impact* approach photometry for assumed values of the spin rate and the spin rate slope. The *Top Panel* shows a harmonics fit with 5 harmonics, and the *Bottom Panel* shows the fit using the DPDM with 60 bins and 5 covers. The grey scale to the left indicates the range of R. Note that in both cases the minimum variance falls well above $d\omega/dt = 0$.

Figure 1

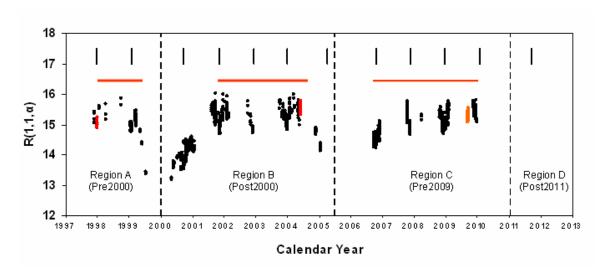


Figure 2

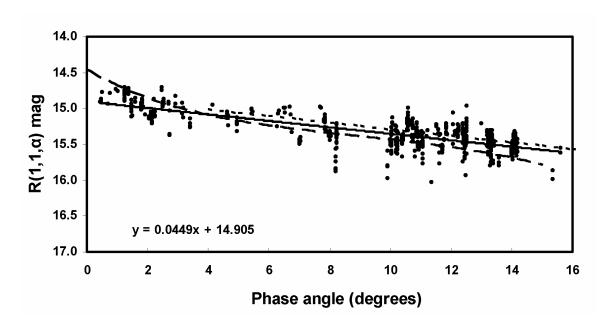


Figure 3

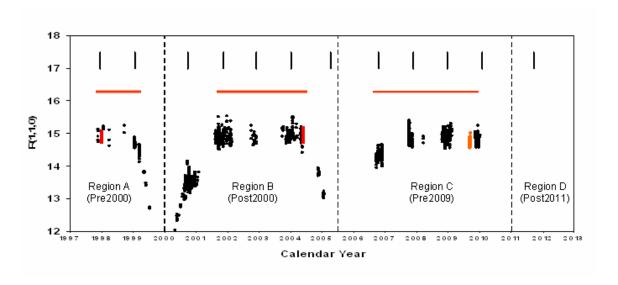


Figure 4

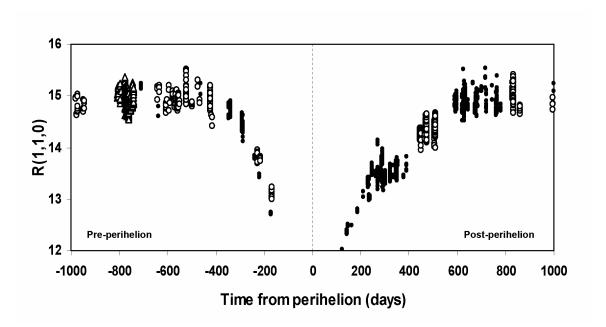


Figure 5

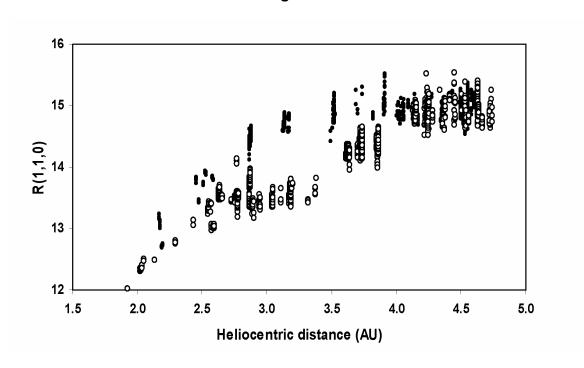


Figure 6

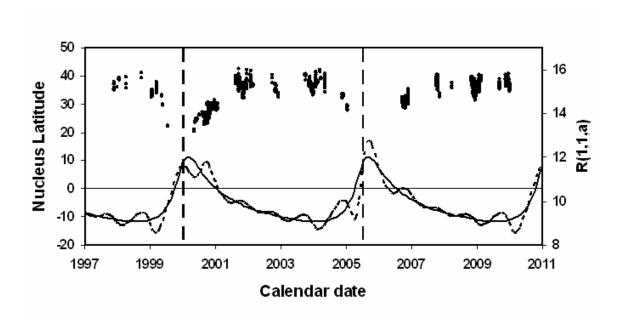


Figure 7

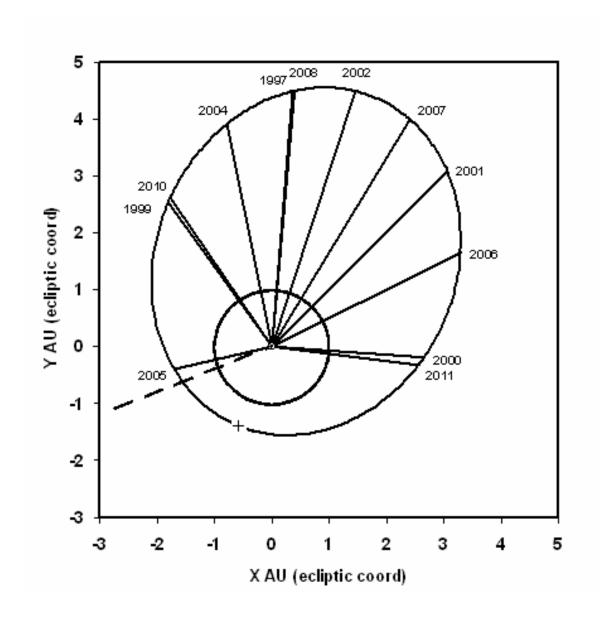


Figure 8

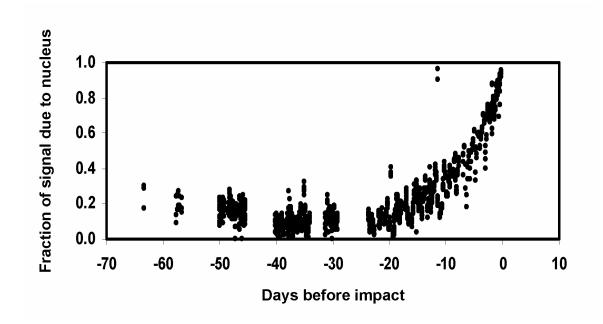


Figure 9

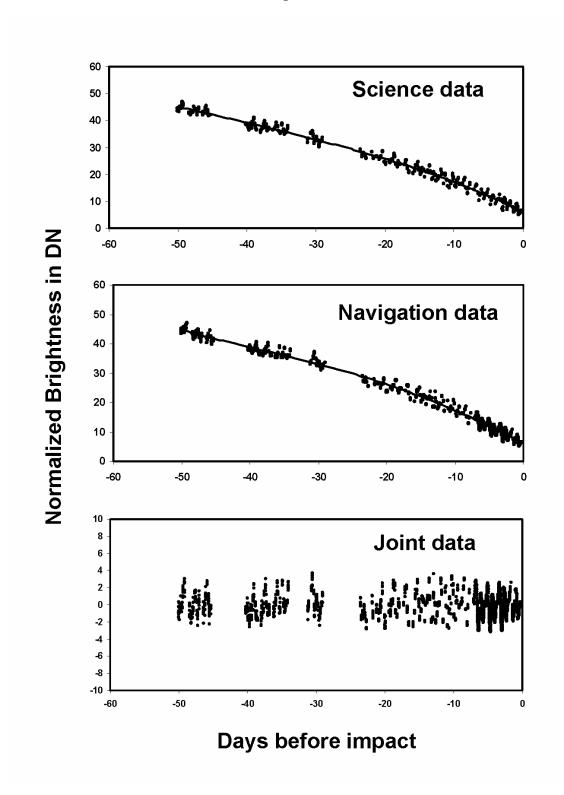


Figure 10

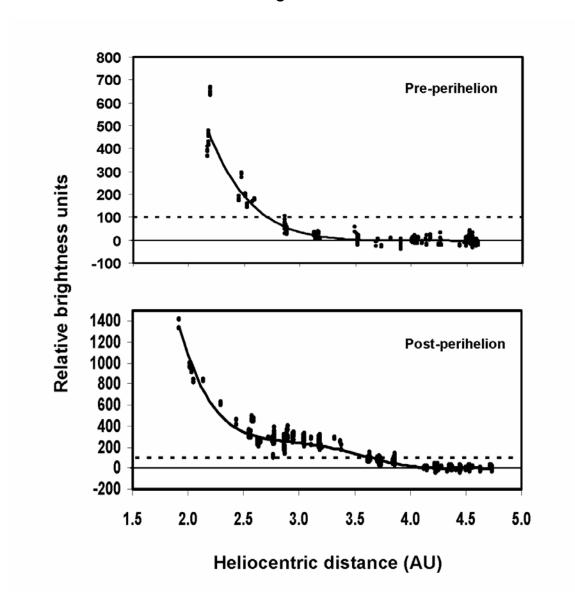


Figure 11

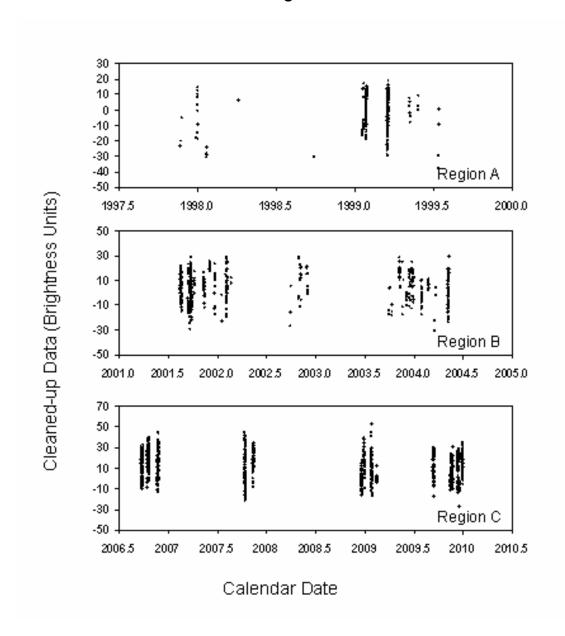
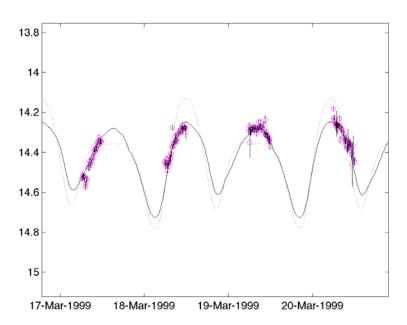


Figure 12





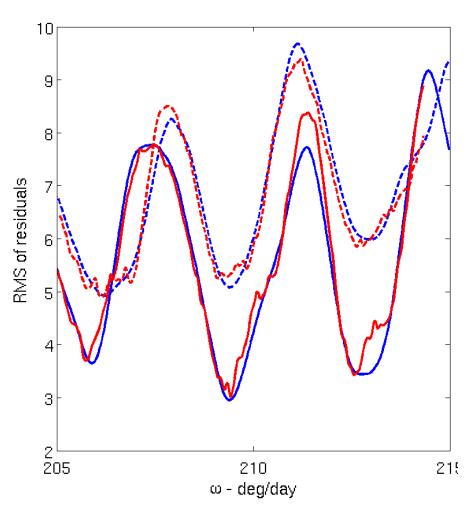


Figure 14

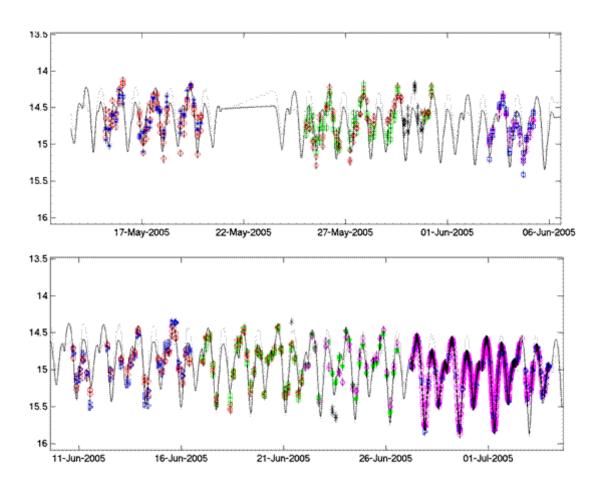


Figure 15

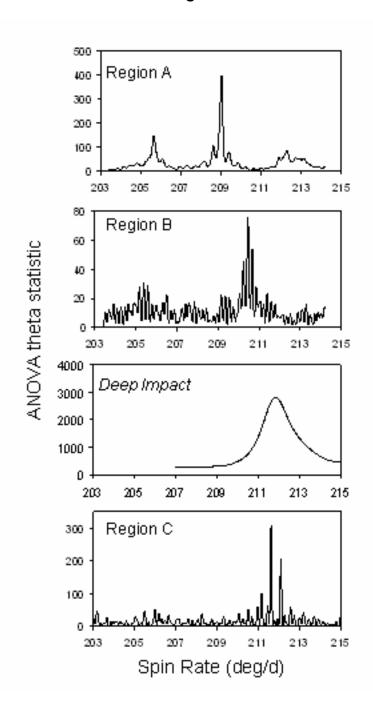


Figure 16

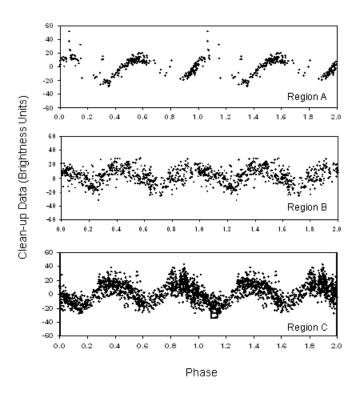
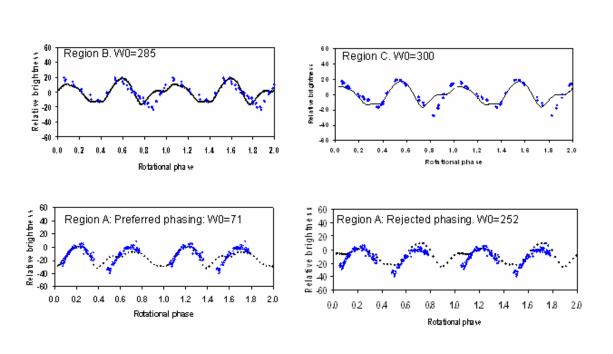


Figure 17



Spin Rate data for 9P/Tempel 1

Figure 18

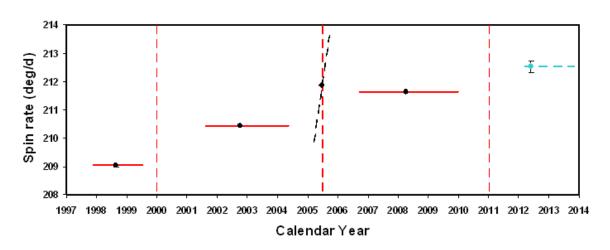


Figure 19

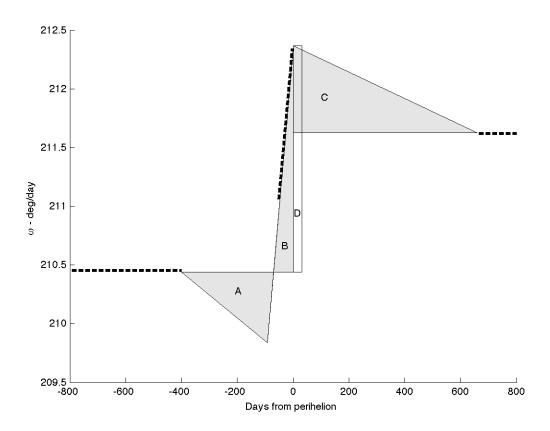


Figure 20

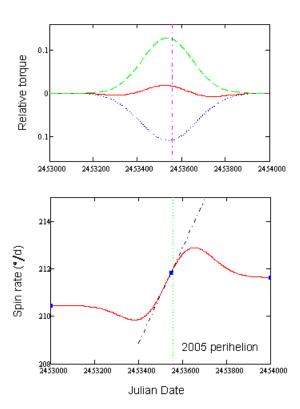


Figure 21

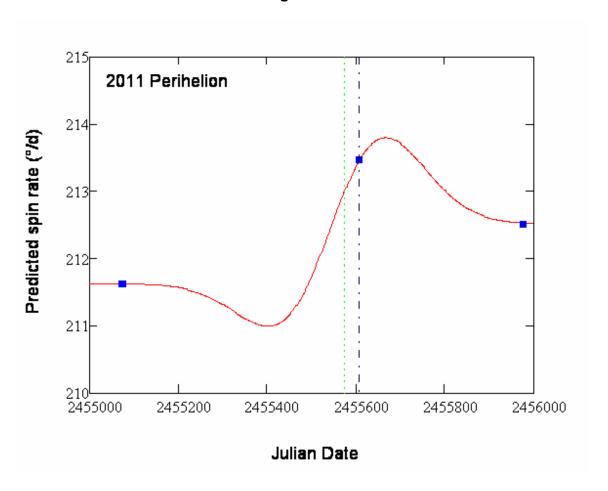


Figure 22

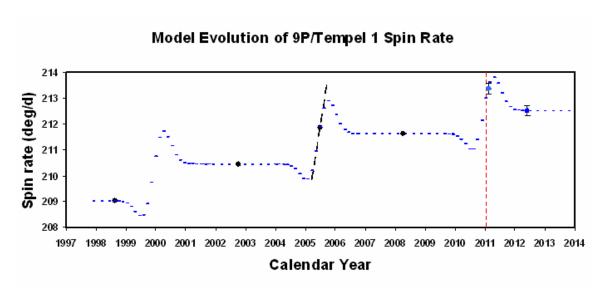
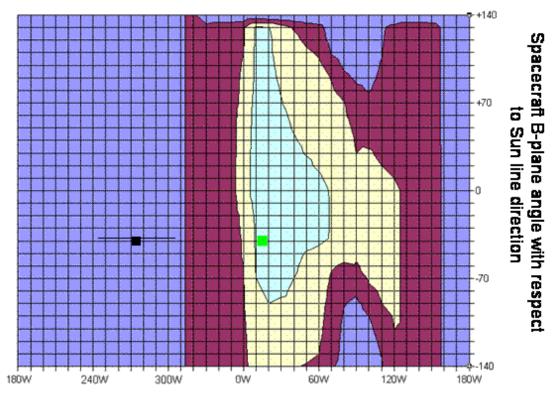


Figure 23



Sub-solar longitude at time of closest approach

Figure 24

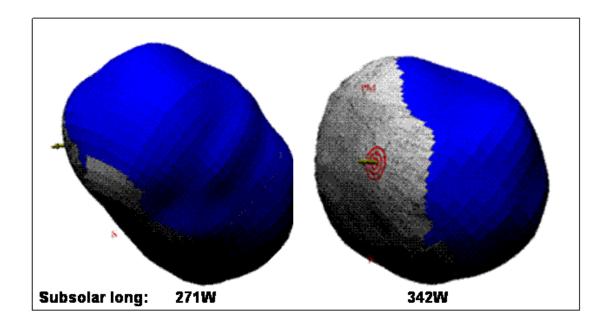


Figure A1

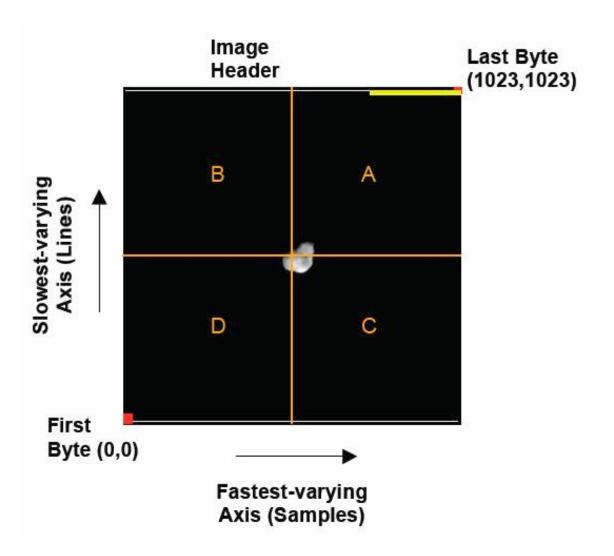


Figure A2

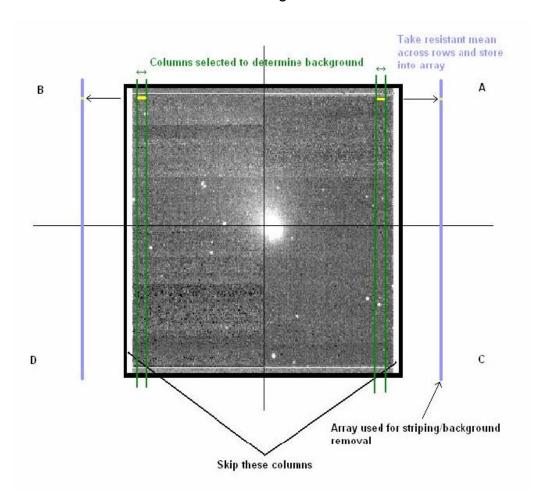


Figure A3

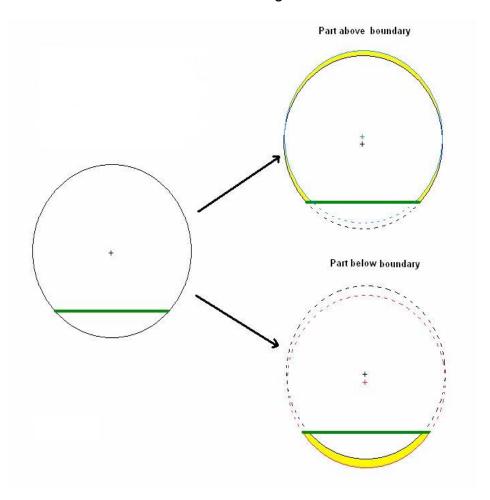


Figure B1

